

Disc Formation in Turbulent Cloud Cores

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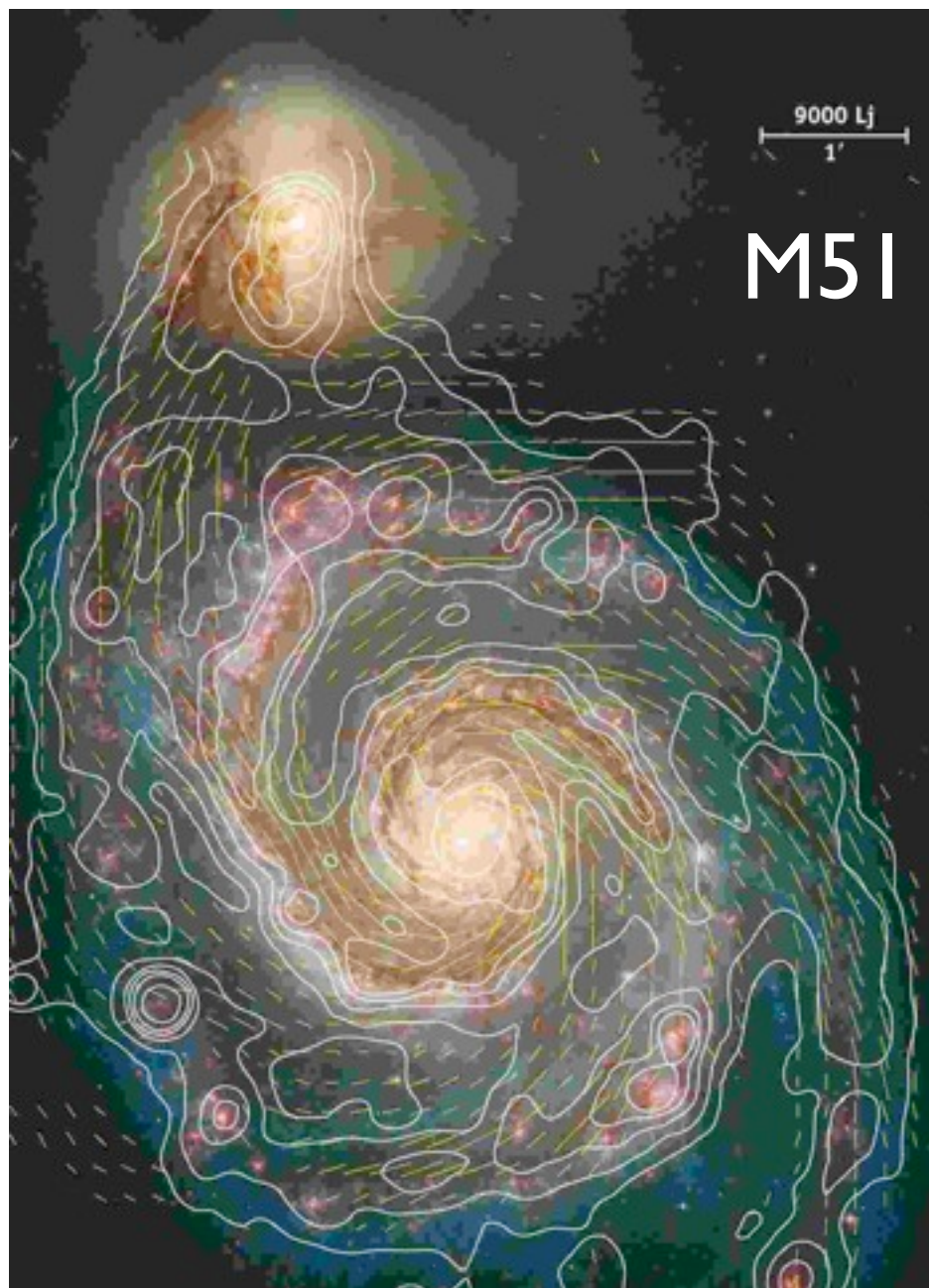




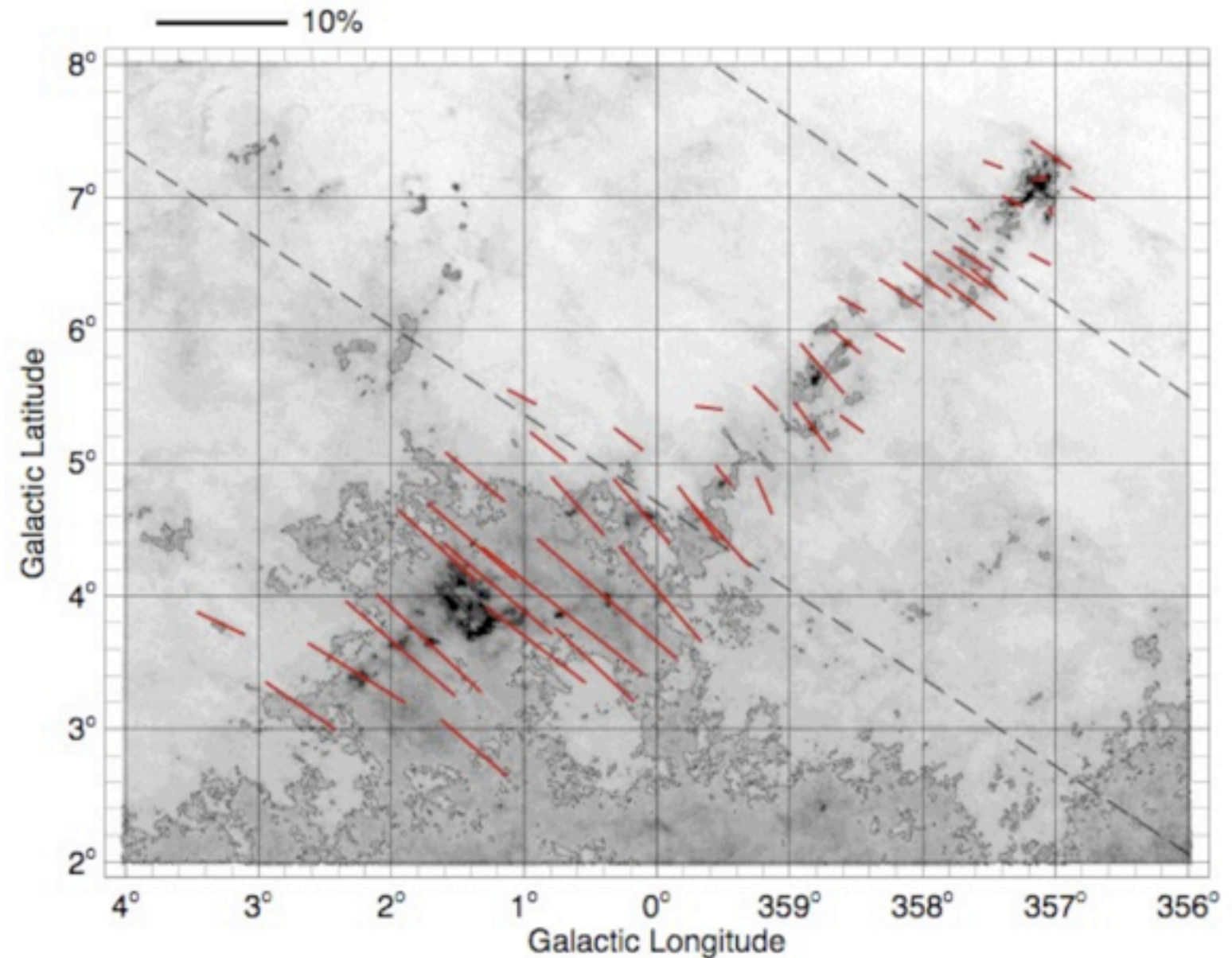
Proplyds (protoplanetary discs) in Orion, *HST*

Magnetic Fields

The ISM is permeated with magnetic fields

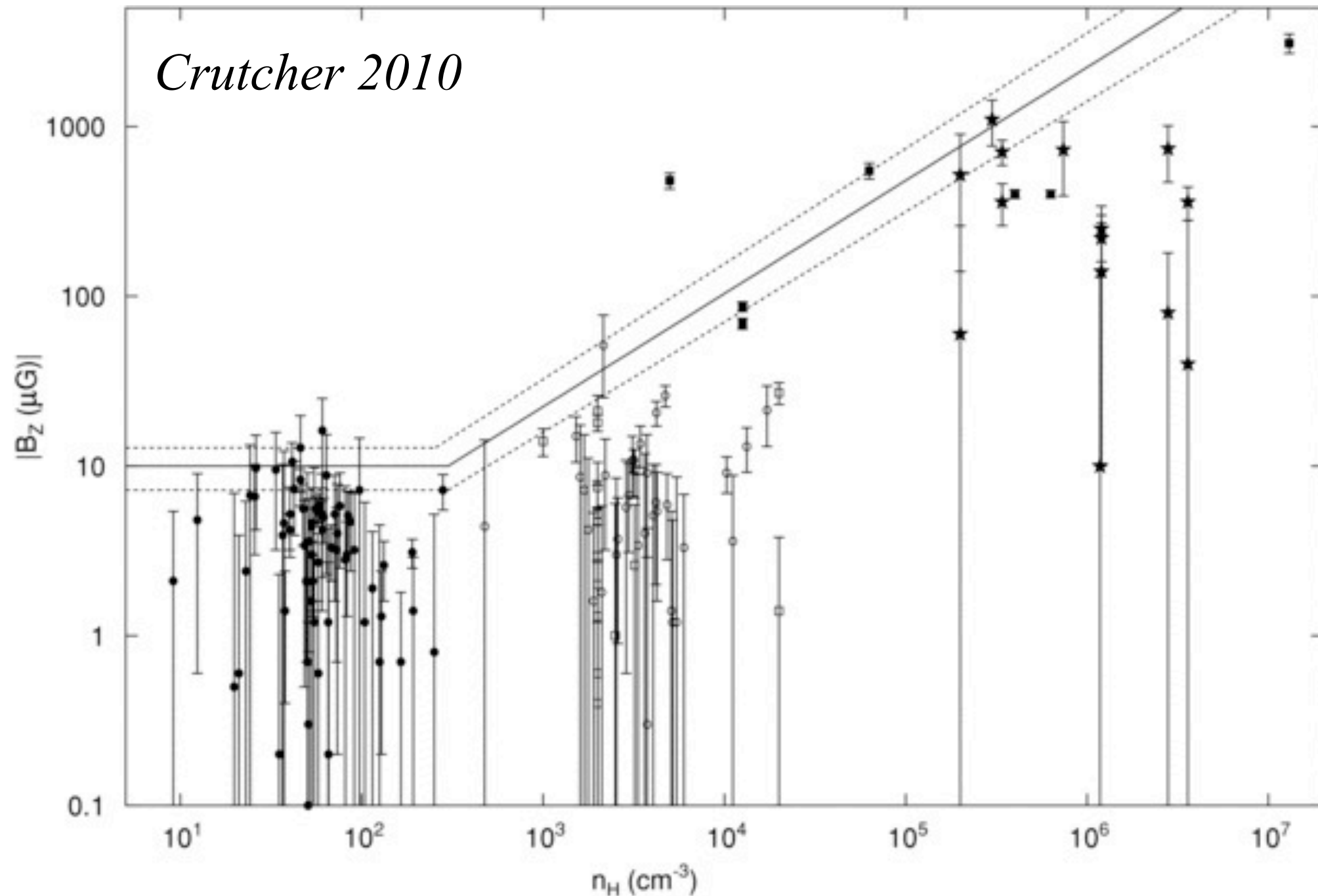


galactic B-fields (e.g. *R.Beck 2001*)
large scale component: $\sim 4\mu\text{G}$
total field strength: $\sim 10\mu\text{G}$



magnetic polarization measurements in the Pipe nebula
F.O.Alves, Franco, Girart 2008

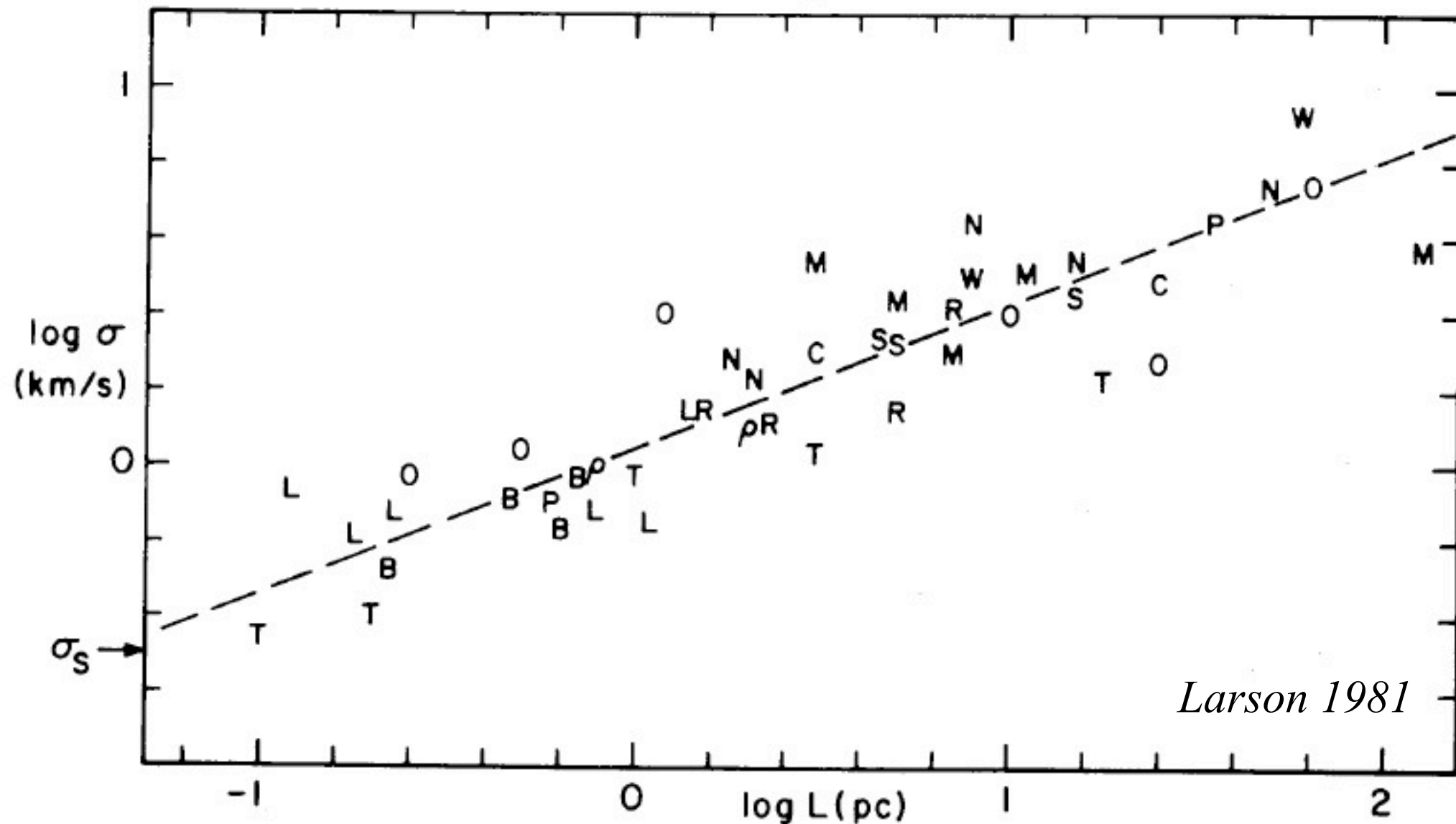
Magnetic Fields



$\Rightarrow$ mass-to-flux ratio for pre-stellar cores:
 $\mu = 2 \dots 5$

Turbulence

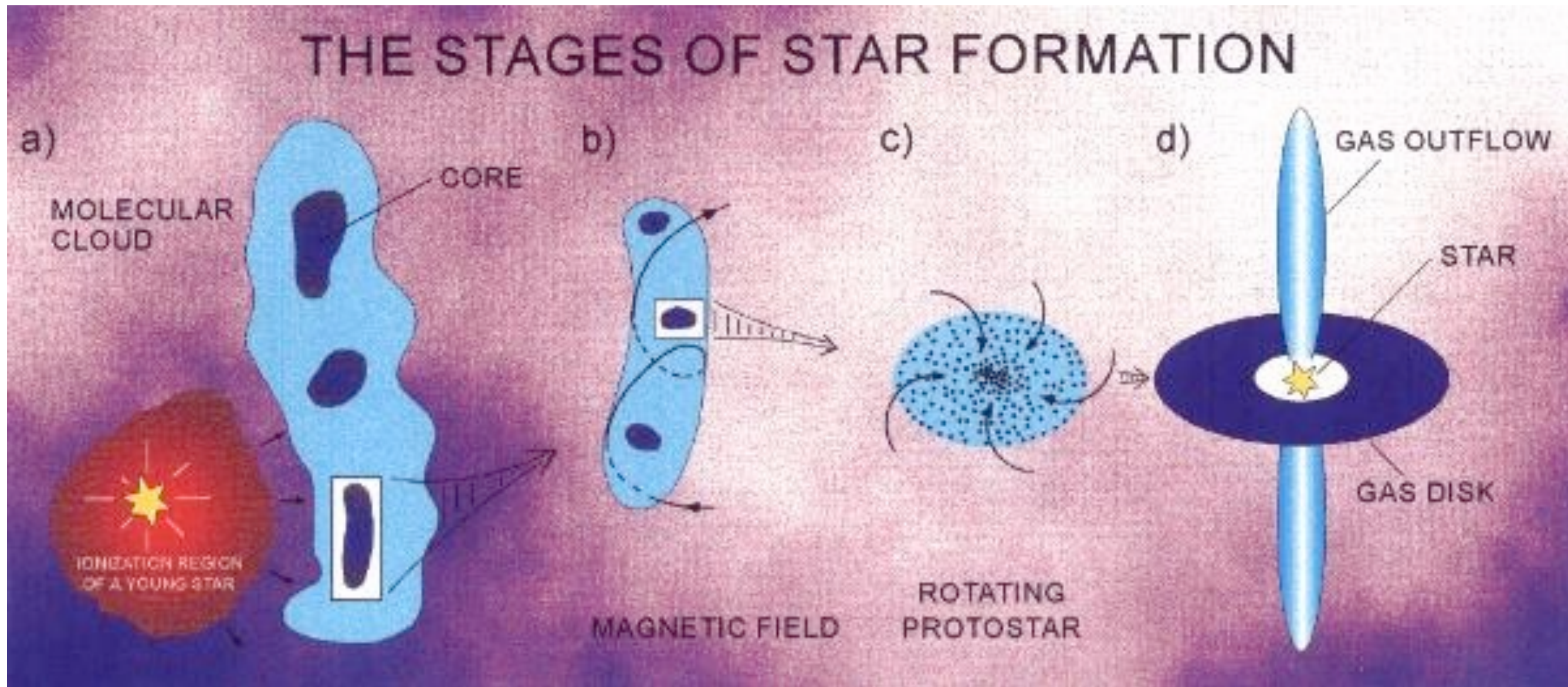
Larson relation: Turbulence in Molecular Clouds



⇒ supersonic high mass cores

⇒ sub-sonic low mass cores ($R < 0.1$ pc)

Star Formation: Early-type discs



Initial angular momentum of cores

- observational evidence for rotating cores ($R \sim 0.1$ pc)
e.g. *Goodman et al., 1993*:

$$\Omega \sim 10^{-14} - 10^{-13} \text{ s}^{-1}$$

$$\Rightarrow j \sim 10^{21} \text{ cm}^2 \text{ s}^{-1}$$

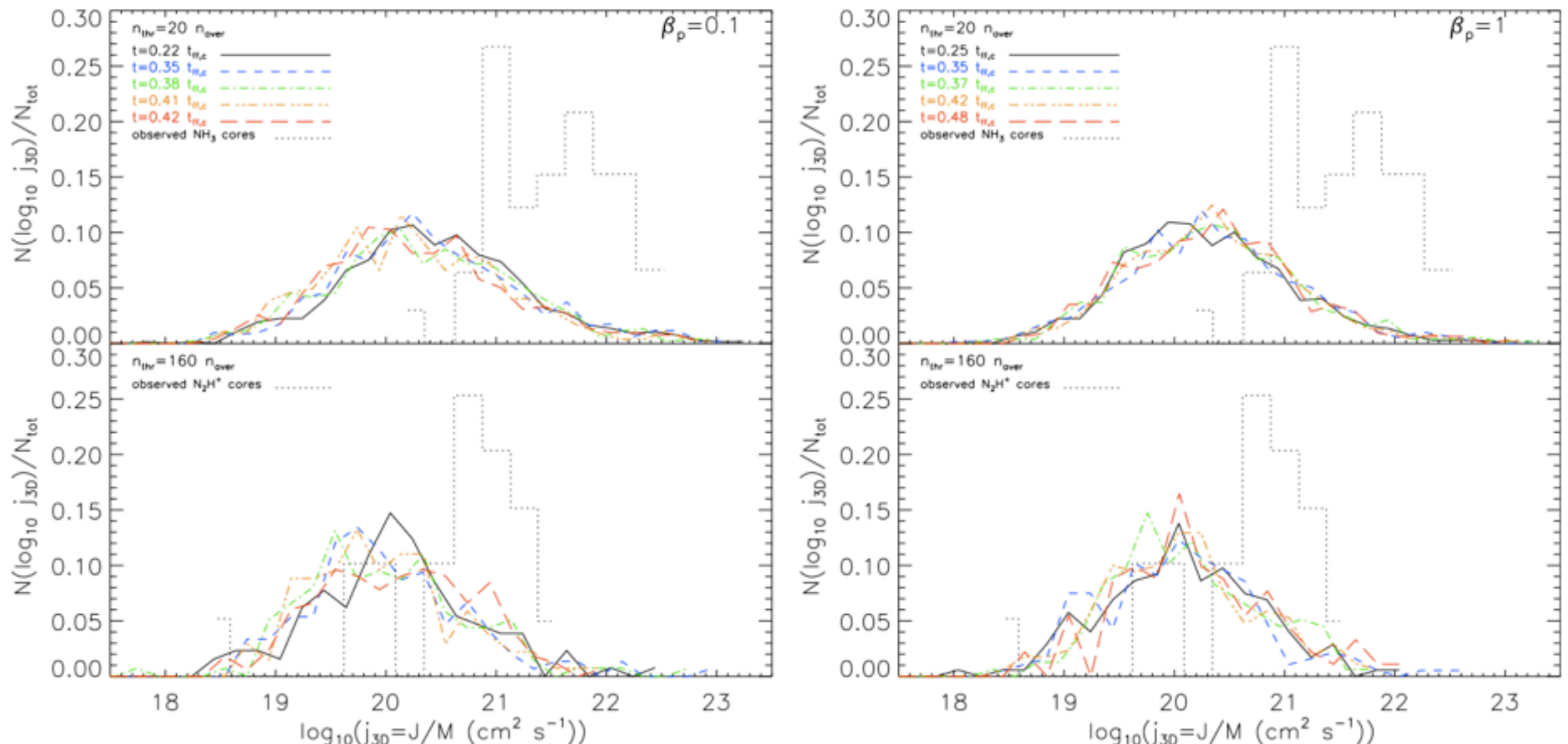
$$\Rightarrow \beta \sim 0.03 \propto (t_{\text{ff}} \Omega)^2$$

but: large scatter

- compare to galactic shear flow: $\Omega \sim 10^{-16} - 10^{-15} \text{ s}^{-1}$
 $\Rightarrow$ generated by **turbulence** (*Barranco & Goodman, 1998*)

Initial angular momentum of cores?

- Dib et al. 2010:
synthetic observations from simulations overestimate
true values by a factor of **8–10**



Angular momentum

- compare to solar system:
 - $j \sim 3 \times 10^{20} \text{ cm}^2 \text{ s}^{-1}$ @ $R = 50 \text{ AU}$
 - $j \sim 4 \times 10^{19} \text{ cm}^2 \text{ s}^{-1}$ @ $R = 1 \text{ AU}$
- Sun: $j \sim 10^{16} \text{ cm}^2 \text{ s}^{-1}$

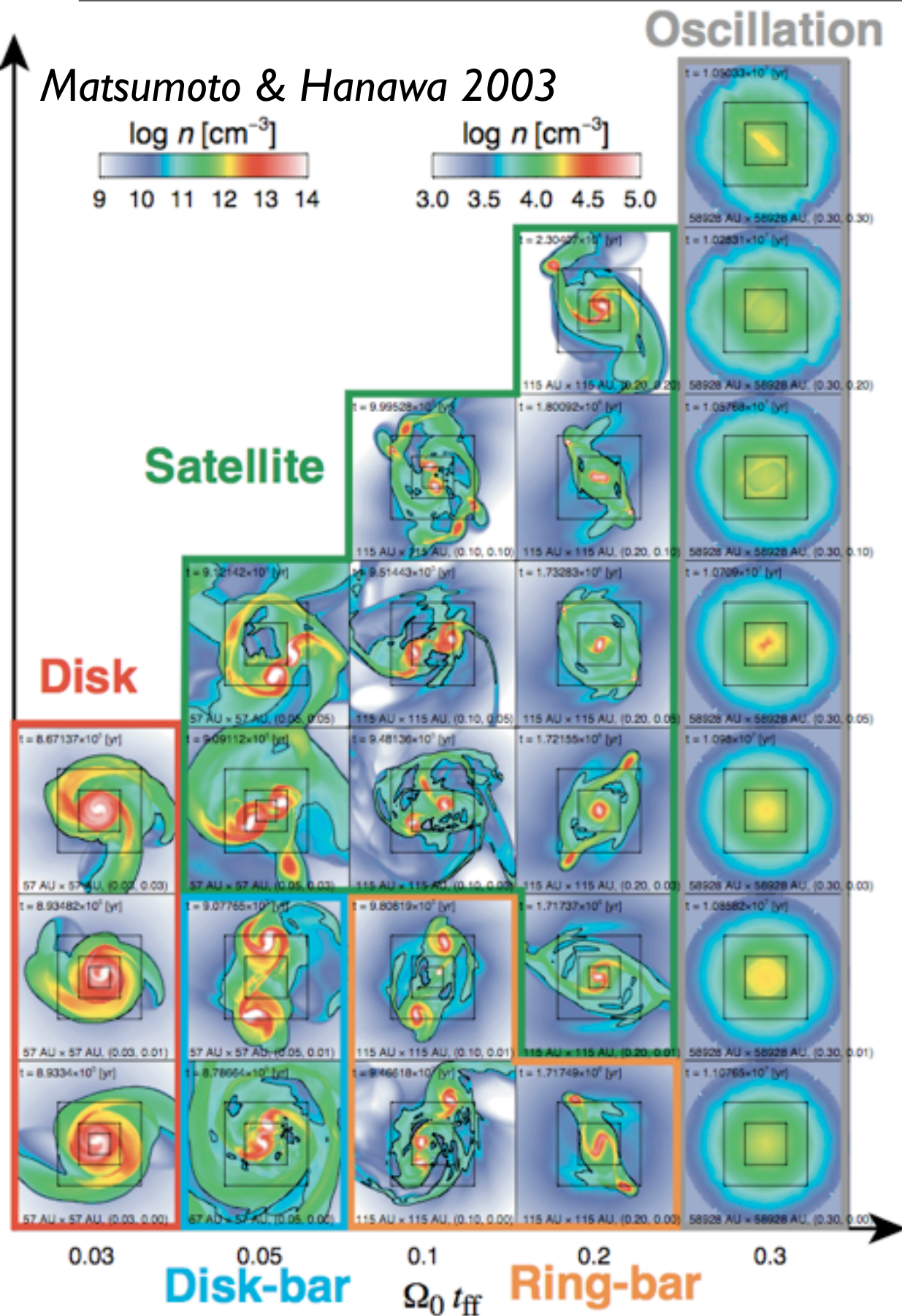
Angular momentum

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⇒ angular momentum transport in the disc needed:

angular momentum problem I

Angular Momentum Problem I



The pure hydro cases

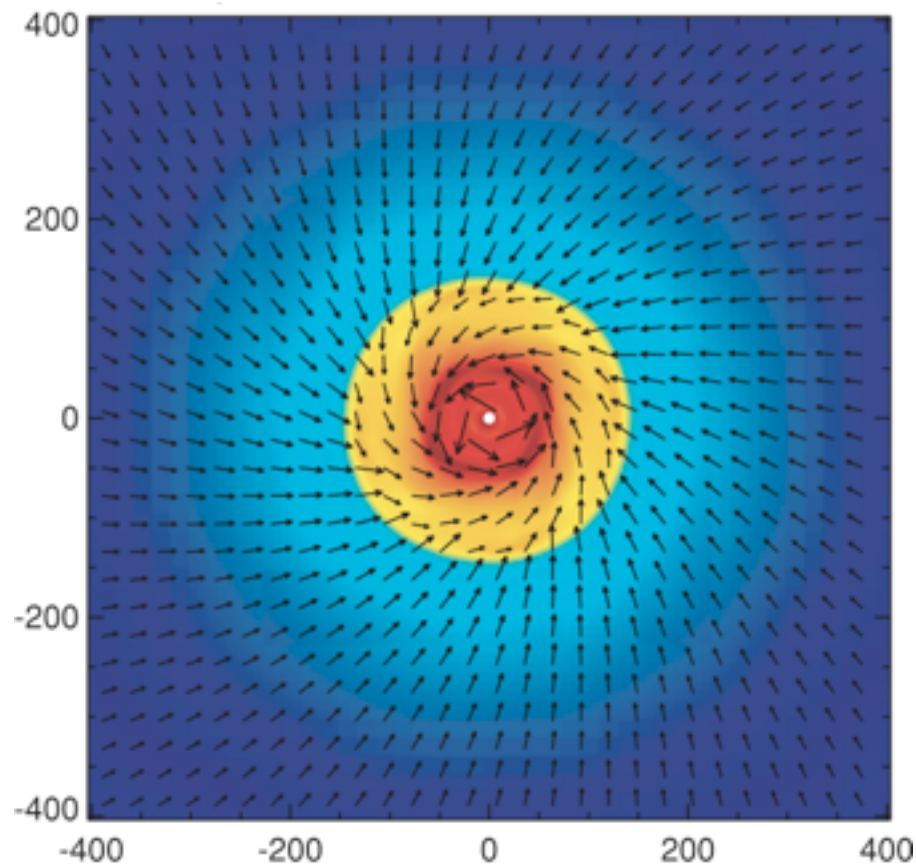
(e.g. Burkert & Bodenheimer 1993, Matsumoto & Hanawa 2003, Krumholz et al. 2007, Stamatellos & Whitworth 2009, ...)

⇒ efficient transport of angular momentum by **gravitational torques**

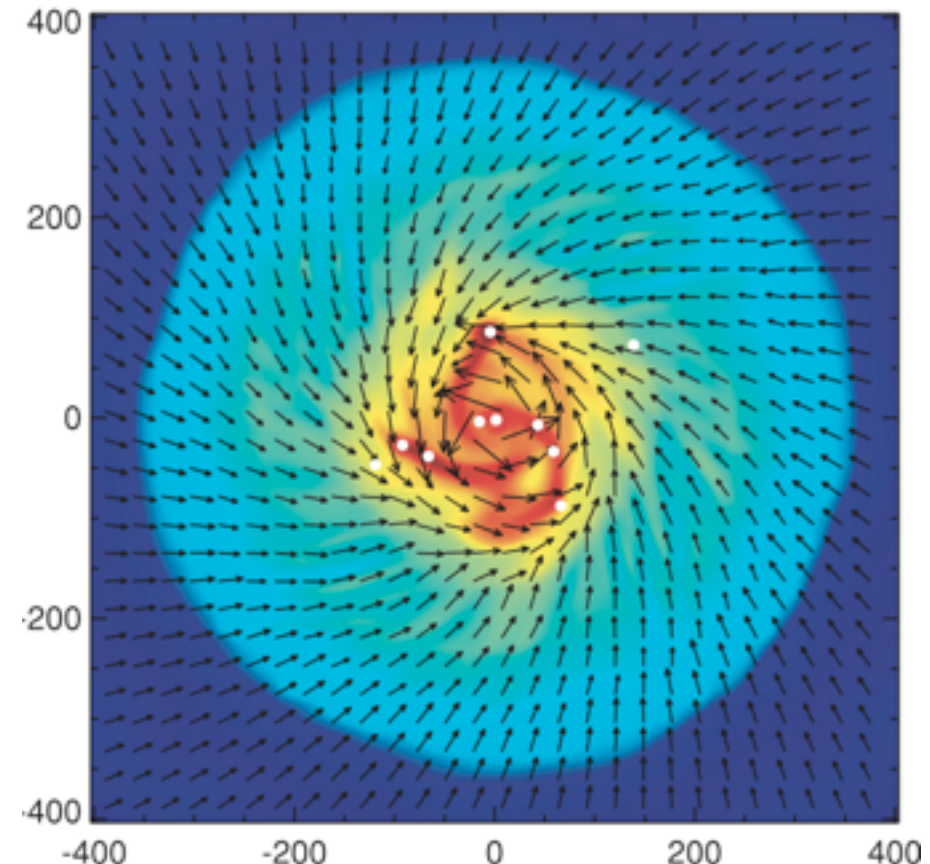
Angular Momentum Problem I

Collapse of **magnetised**, rotating cloud cores

- **weak** magnetic fields: $\mu > 10$



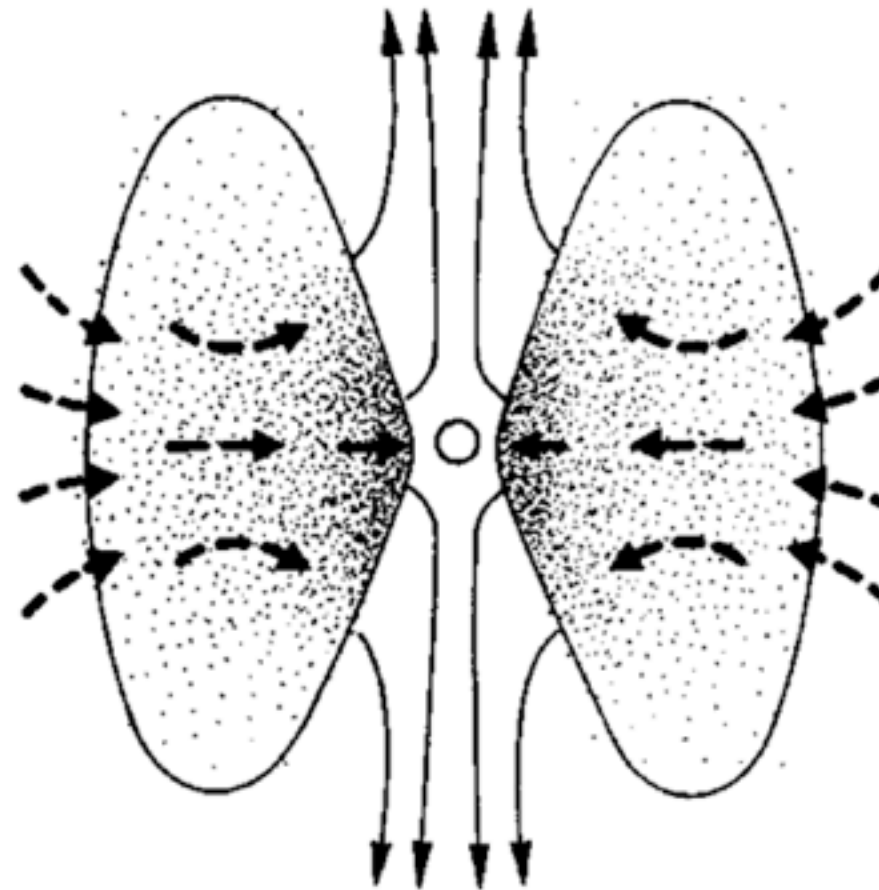
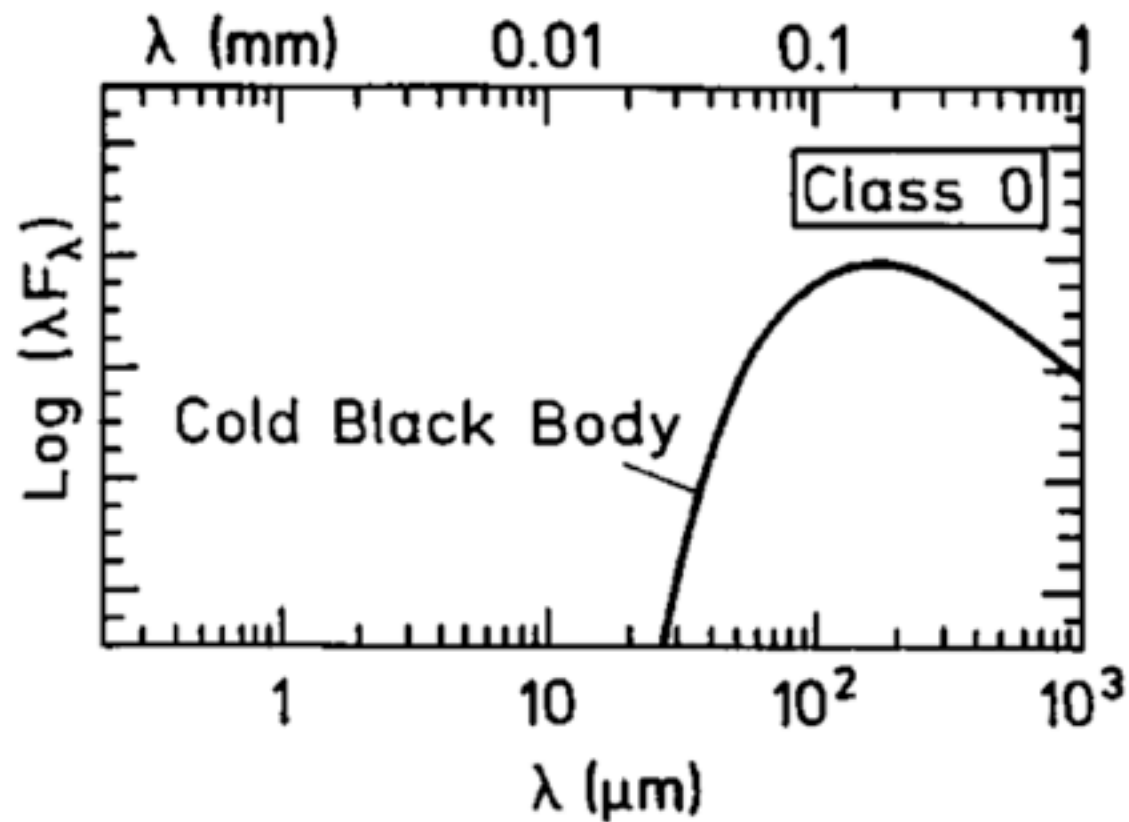
+ 1000 yr
→



Seifried et al. 2011

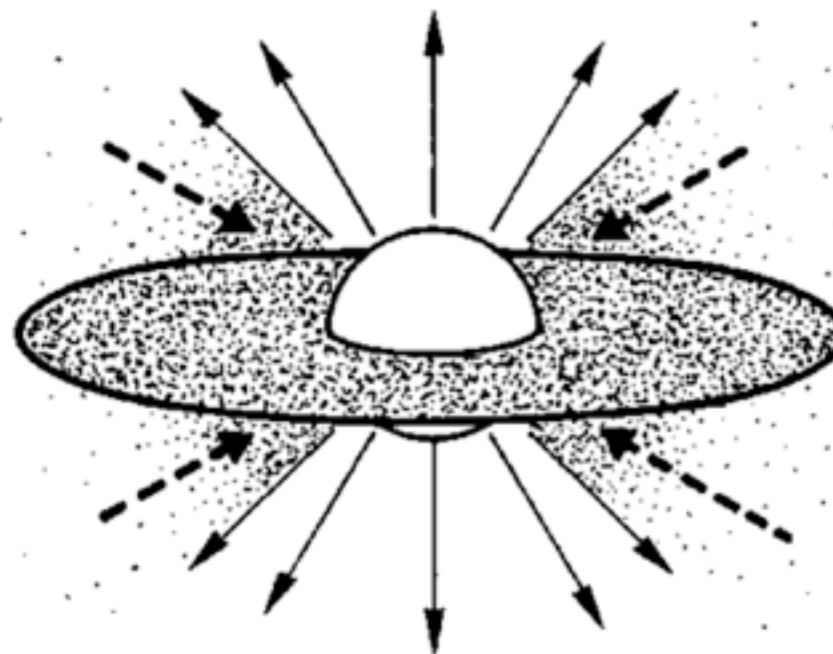
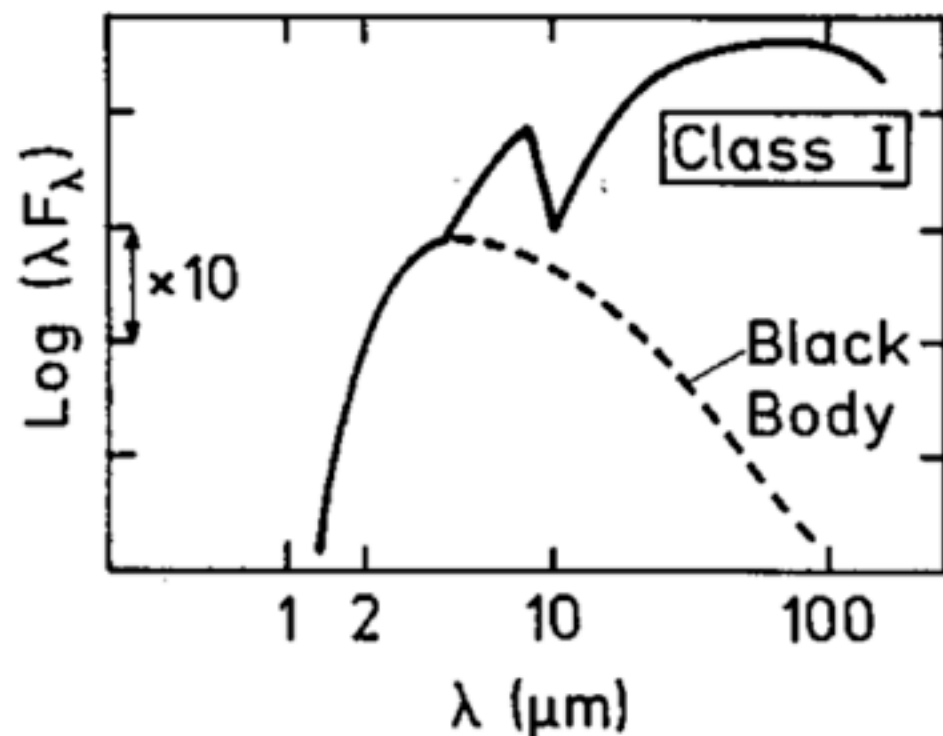
- ⇒ efficient transport of angular momentum
mainly by gravitational torques / fragmentation
- ⇒ disc formation & high accretion rates $\sim 10^{-4} M_{\odot}/\text{yr}$

Star Formation: Early-type discs



CLASS 0:
*Main
accretion
phase?*

Age $\leq 10^4$ yr
 $M_{\text{C}*} \geq 0.5 M_\odot$



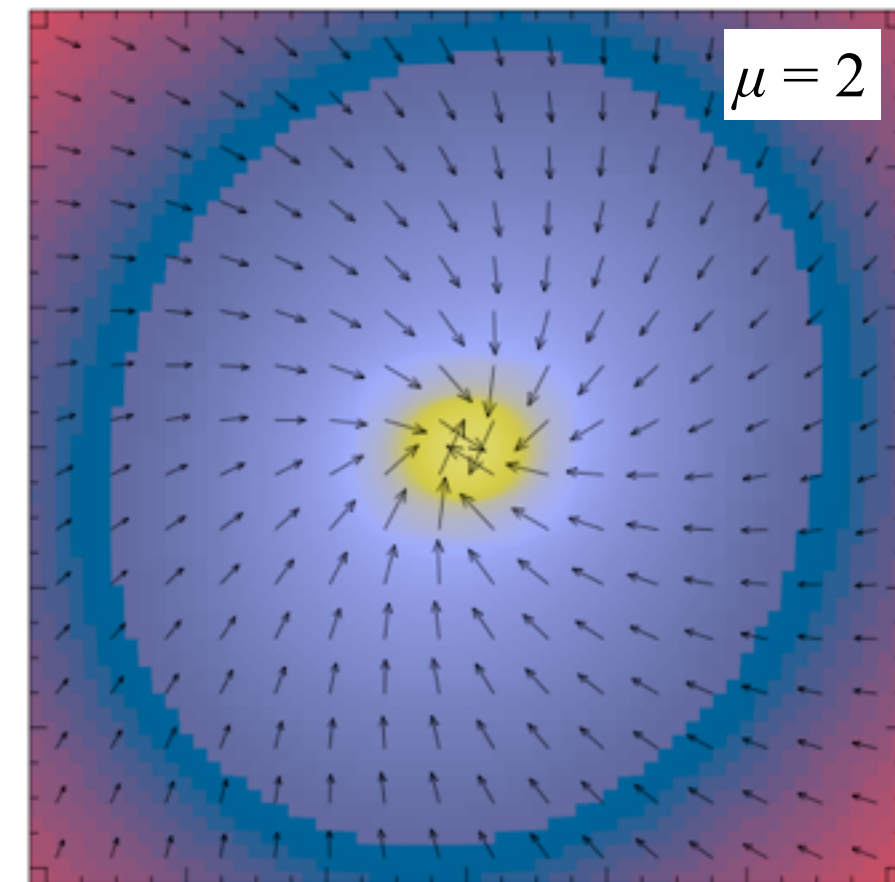
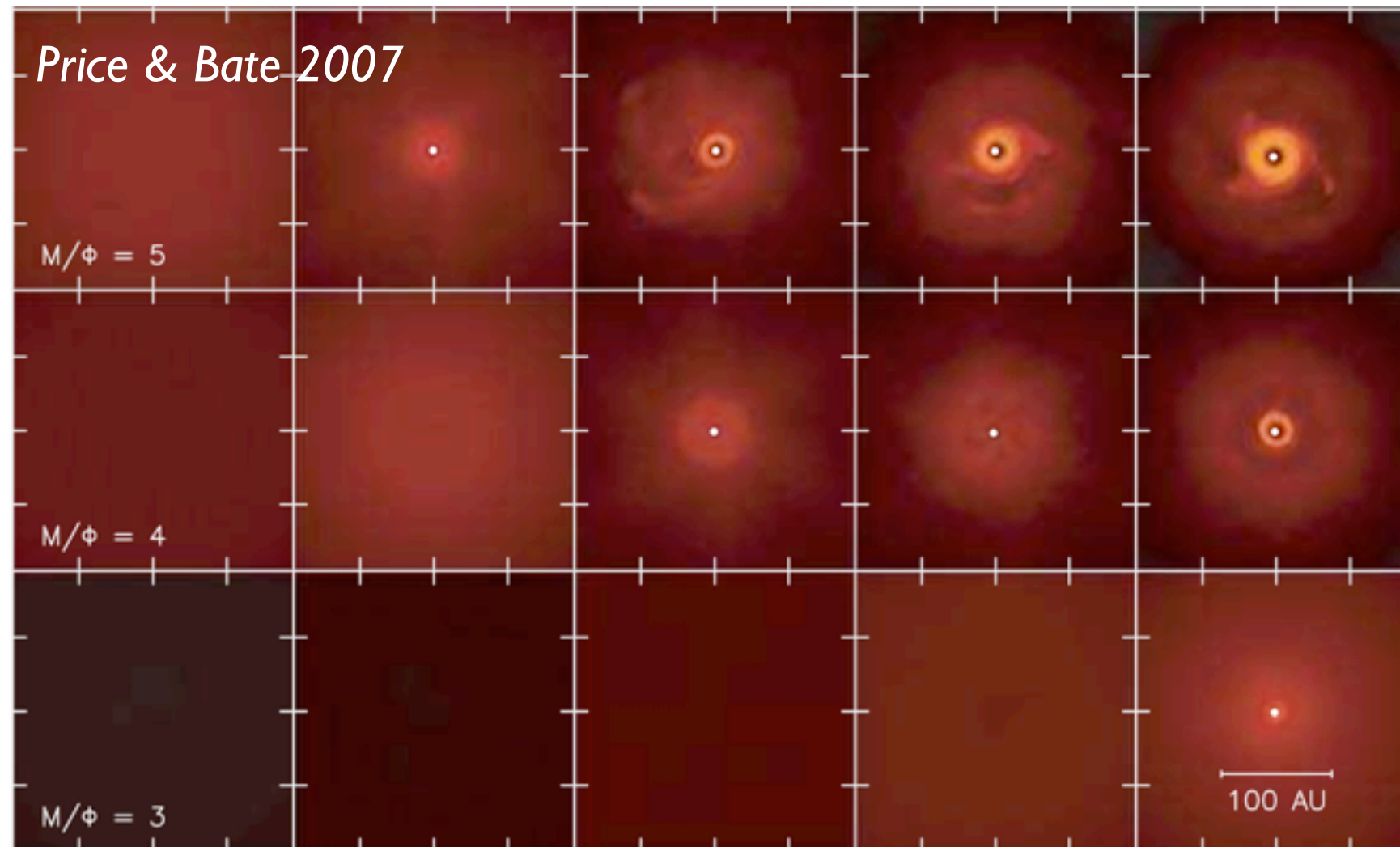
CLASS I:
*Late
accretion
phase?*

Age $\sim 10^5$ yr
 $M_{\text{C}*} \lesssim 0.1 M_\odot$

Star Formation: Early-type discs

Collapse of magnetised, rotating cloud cores

- **stronger** magnetic fields: $\mu < 5$ in agreement with observations
(e.g. *Crutcher et al. 2010*)



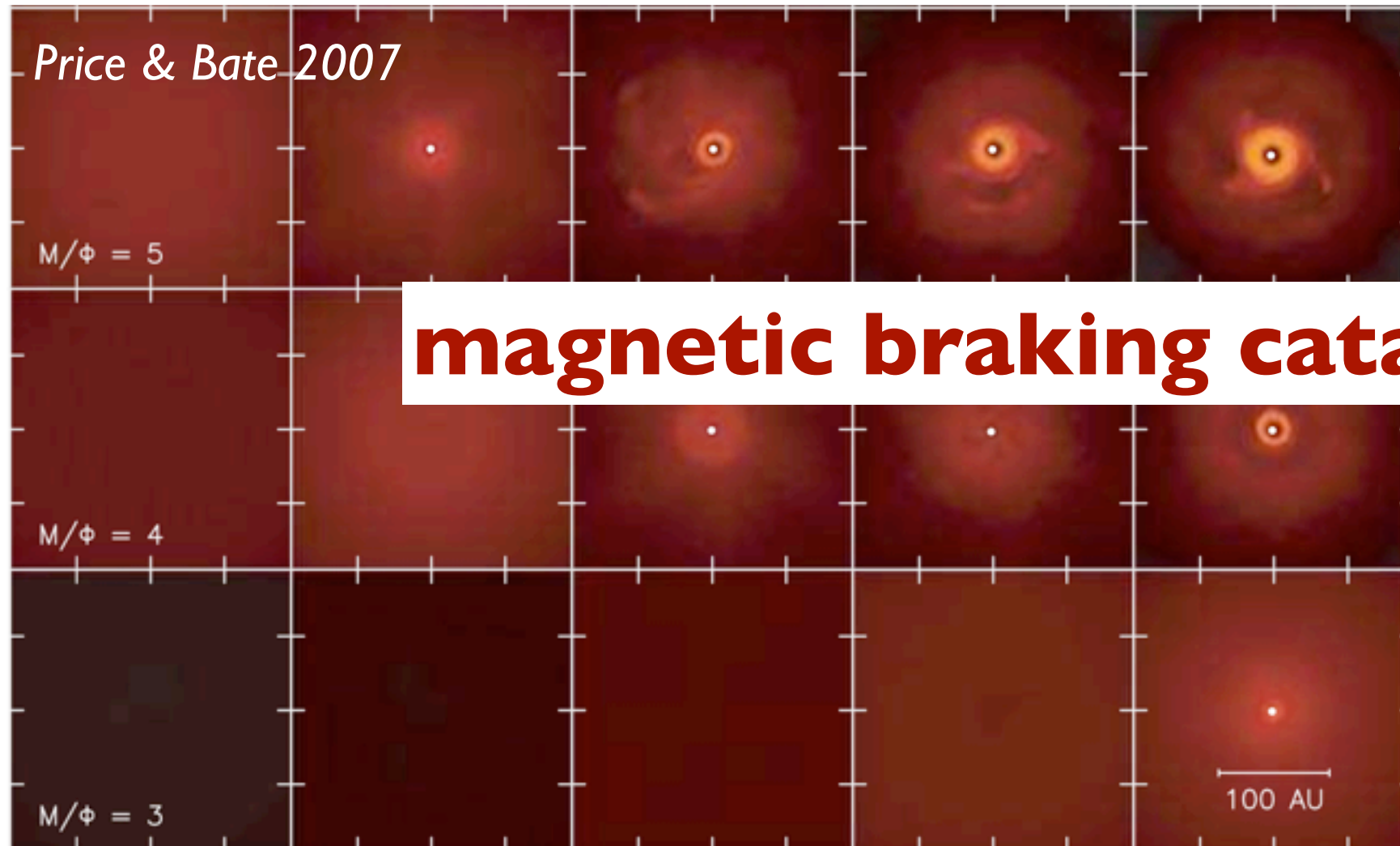
Hennebelle & Teyssier 2008, ...

⇒ **too** efficient magnetic braking
⇒ **no** disc formation

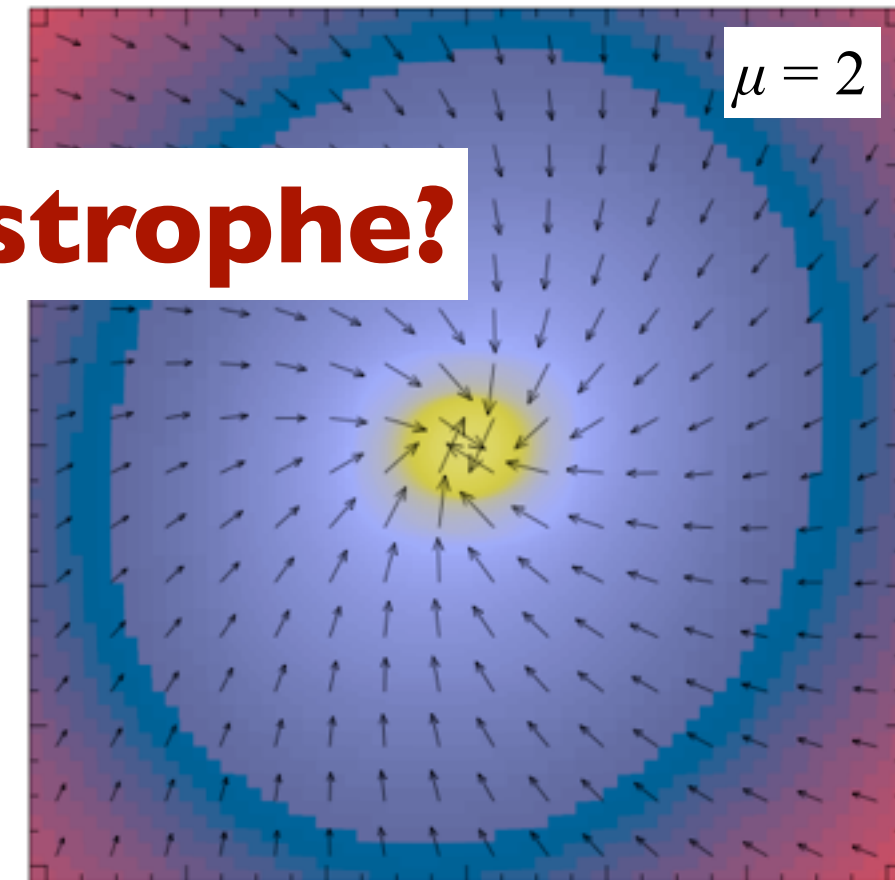
Star Formation: Early-type discs

Collapse of magnetised, rotating cloud cores

- **stronger** magnetic fields: $\mu < 5$ in agreement with observations
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magnetic braking catastrophe?



Hennebelle & Teyssier 2008, ...

- ⇒ **too** efficient magnetic braking
- ⇒ **no** disc formation

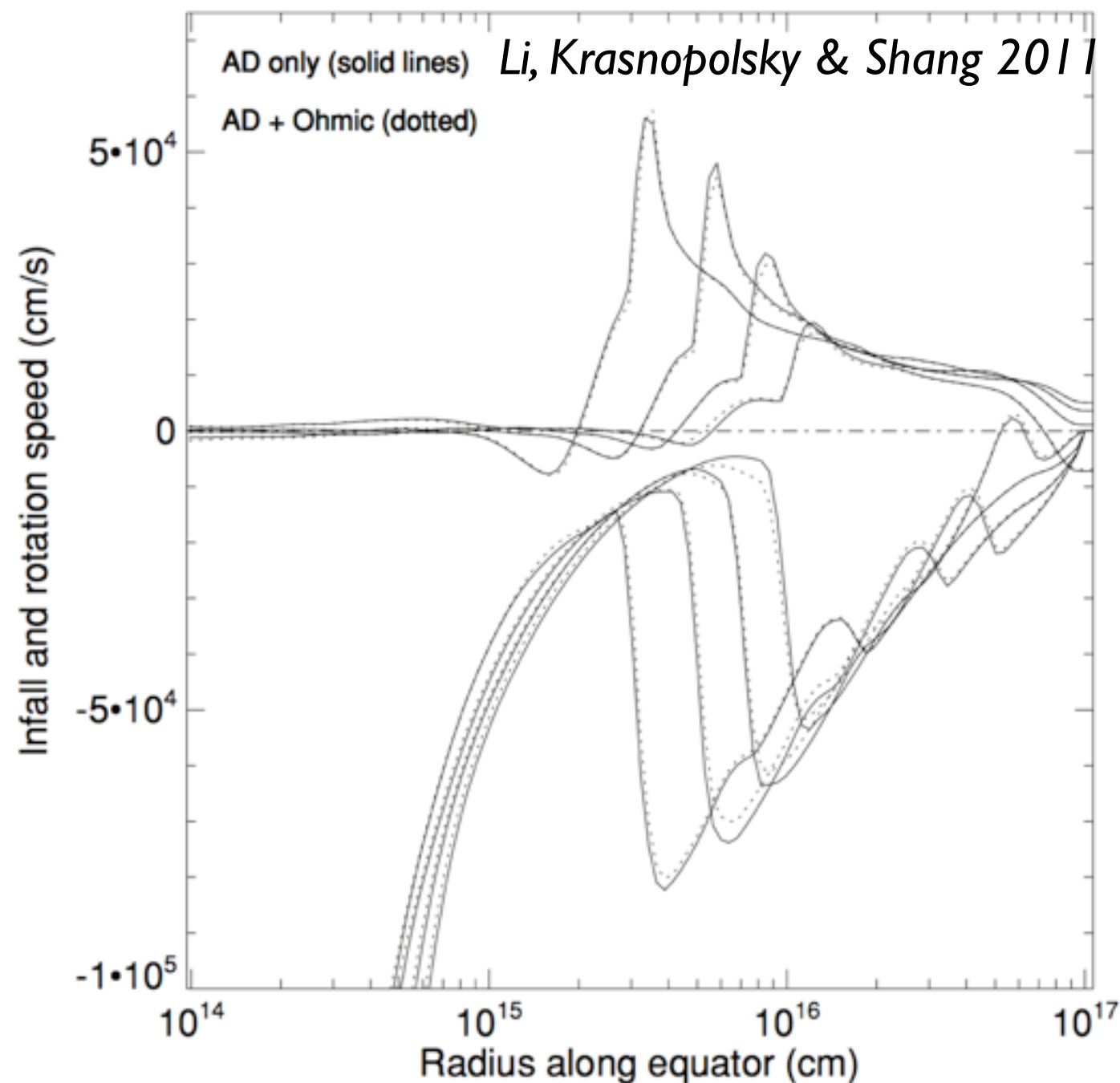
Angular Momentum Problem II

Solutions?

- flux loss by:
 - Ohmic resistivity (*Dapp & Basu 2011, Krasnopolsky et al. 2010*)
 - ambipolar Diffusion (*Duffin & Pudritz 2008, Li et al. 2011*)
 - turbulent reconnection
(*Lazarian & Vishniac 1999, Santos-Lima et al. 2012*)
- Hall effect (*Krasnopolsky et al. 2011*)
- Outflows from small discs

Angular Momentum Problem II

- ⇒ Non-ideal MHD and reconnection active only at small scales/high density
- ⇒ not effective enough to reduce magnetic braking



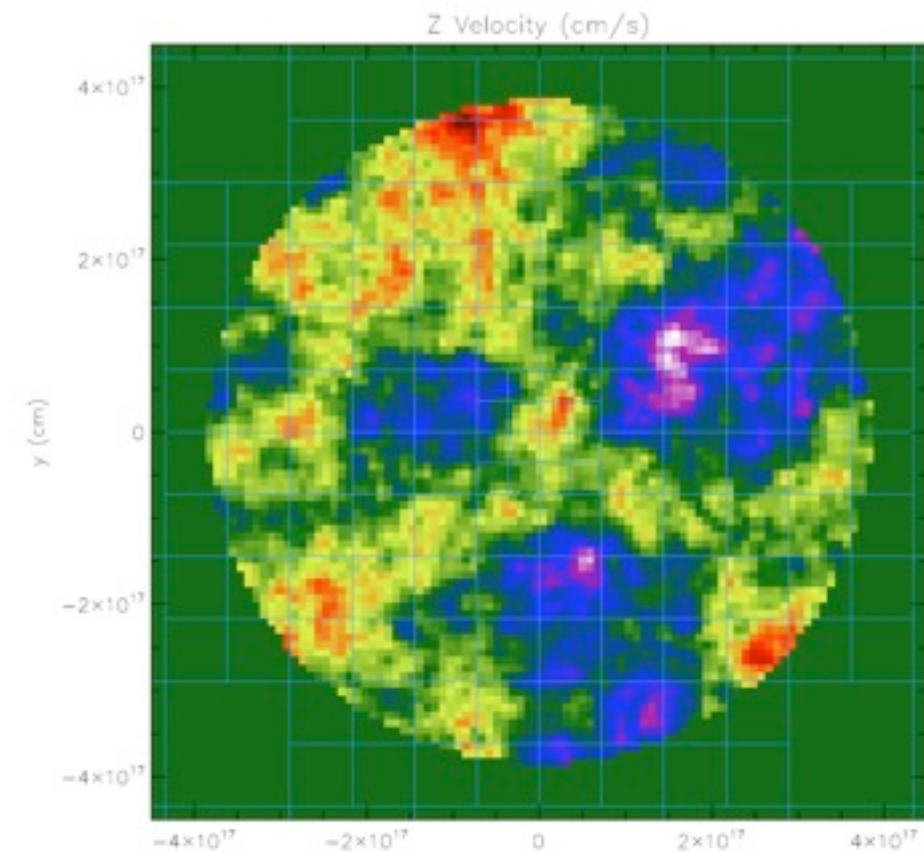
⇒ *Li, Krasnopolsky & Shang 2011*:
“The problem of catastrophic magnetic braking that prevents disk formation in dense cores magnetized to realistic levels remains unresolved”

Parameter study of collapsing cores

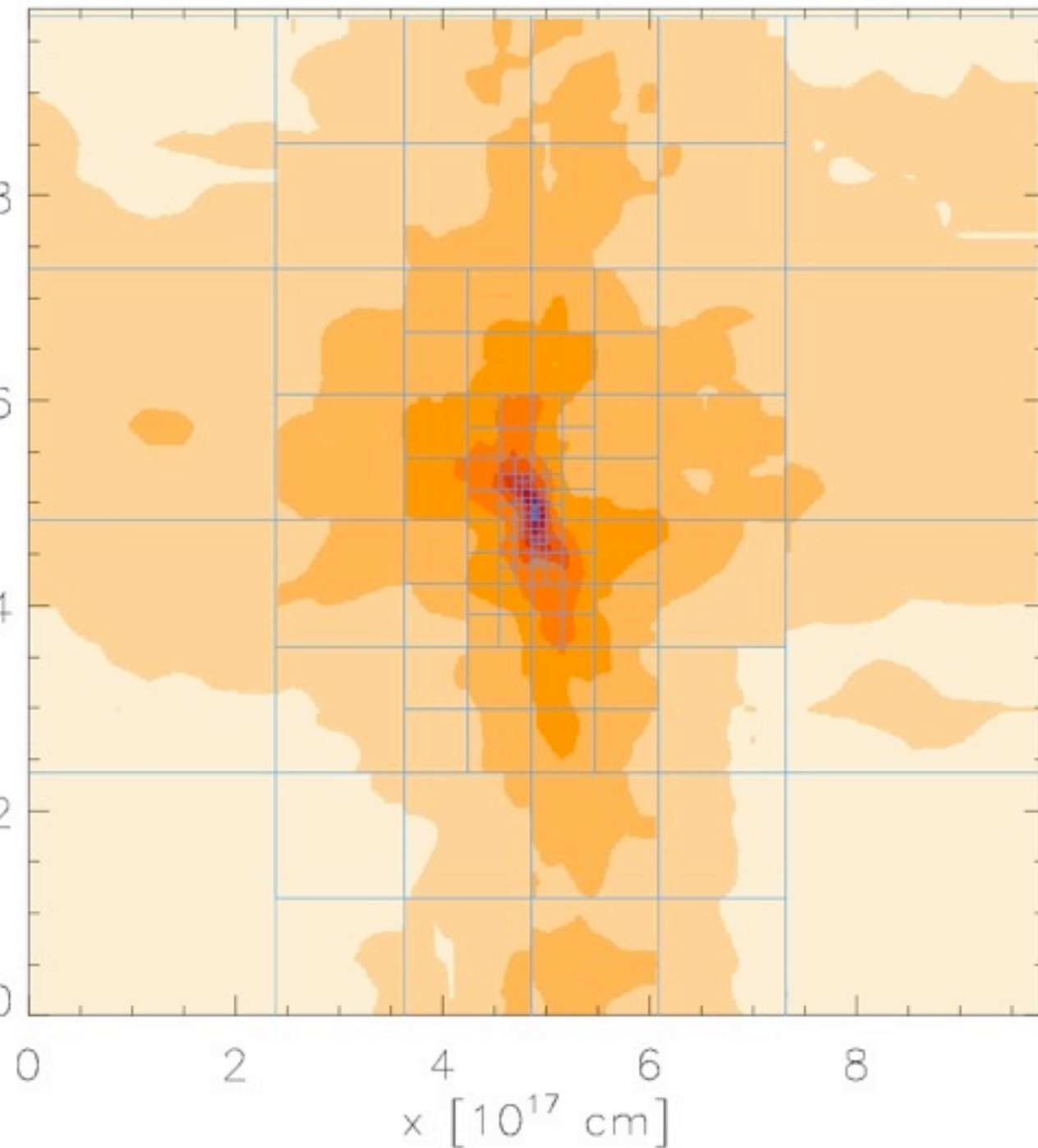
Seifried, et al. 2013

Run	m_{core} ($M_{\odot}$)	r_{core} (pc)	μ	Rotation	Ω (10^{-13} s^{-1})	β_{turb}	Turbulence seed	p	M_{rms}	t_{sim} (kyr)
2.6-NoRot-M2	2.6	0.0485	2.6	No	0	0.087	A	5/3	0.74	15
2.6-Rot-M2	2.6	0.0485	2.6	Yes	2.20	0.087	A	5/3	0.74	15
2.6-NoRot-M100	100	0.125	2.6	No	0	0.084	A	5/3	2.5	15
2.6-Rot-M100	100	0.125	2.6	Yes	3.16	0.084	A	5/3	2.5	15
2.6-Rot-M100-B	100	0.125	2.6	Yes	3.16	0.084	B	5/3	2.5	15
2.6-Rot-M100-C	100	0.125	2.6	Yes	3.16	0.084	C	5/3	2.5	15
2.6-Rot-M100-p2	100	0.125	2.6	Yes	3.16	0.084	A	2	2.5	15
2.6-NoRot-M300	300	0.125	2.6	No	0	0.12	A	5/3	5.0	10
2.6-Rot-M1000	1000	0.375	2.6	Yes	1.90	0.081	A	5/3	5.4	10

- low + high mass cores
- strong magnetic field
- with/without global rotation
- sub-/supersonic **turbulence**



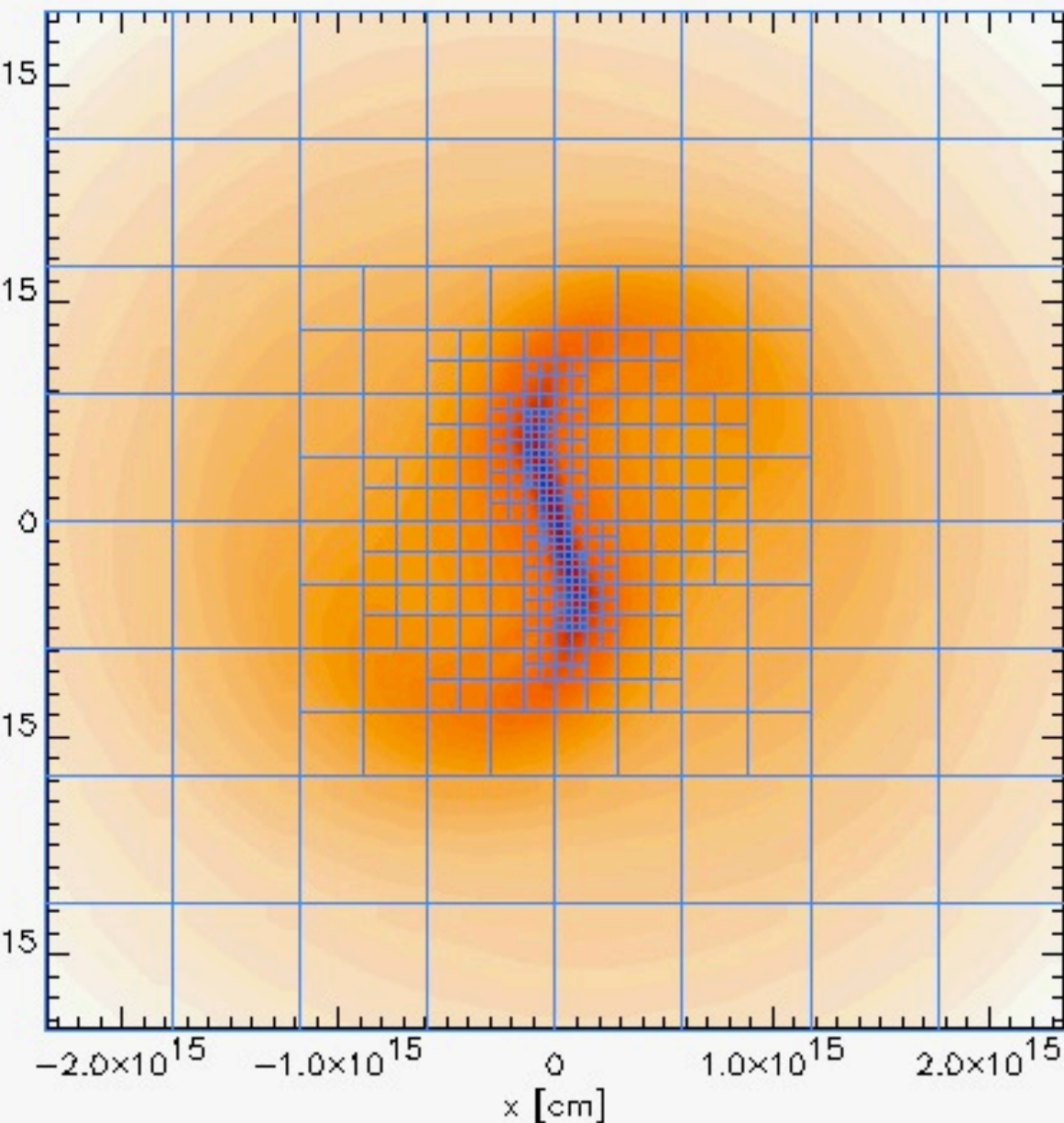
Numerical Method: FLASH Code



**Alliance Center for Astrophysical
Thermonuclear Flashes (ASC),
University of Chicago*

- 3D grid-based MHD integrator for parallel computing (MPI)
- Hydro solvers: PPM, Kurganov
- MHD solvers:
 - 8Wave (Roe-type)
 - **Bouchut-type**
 - also: unsplit scheme, staggered mesh
- Gravity:
 - multigrid
 - multipole
 - **tree-based**
 - periodic or isolated BCs
- Multi-physics:
 - heating/cooling
 - radiation
 - **sink particles**
- **AMR**: block structured (PARAMESH)
- Refinement on own choice (e.g. gradient, curvature, density, **Jeans-criterion**, etc.)

Numerical Method: FLASH Code



Jeans-criterion:

minimum resolution to resolve the Jeans-length (*Truelove et al. 1997*):

$$N = \lambda_J / \Delta x \geq 4$$

- only sufficient to prevent numerical fragmentation
- **higher** resolution necessary to resolve internal structures
Turbulence ~ 30 grid cells
(e.g. *Federrath et al. 2010*)

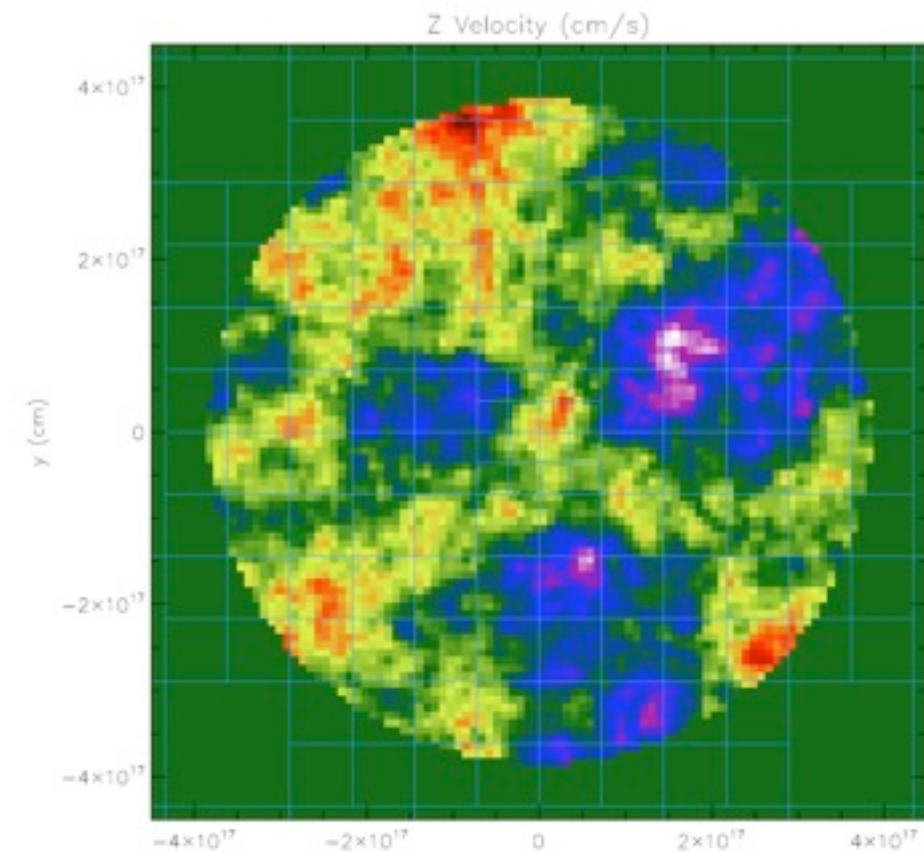
$$\text{Jeans-length: } \lambda_J = \sqrt{\frac{\pi c_s^2}{G_N \rho}}$$

Parameter study of collapsing cores

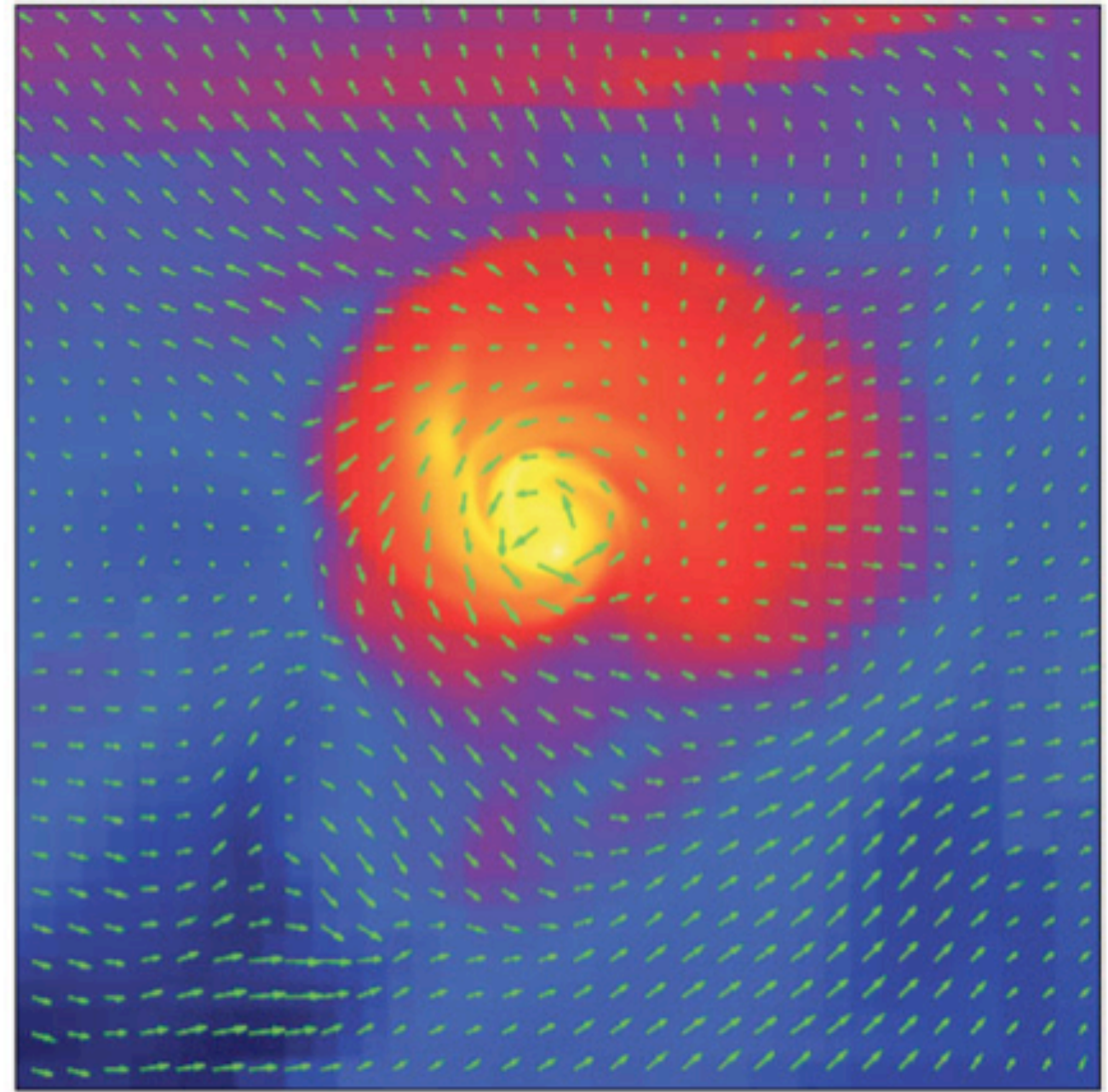
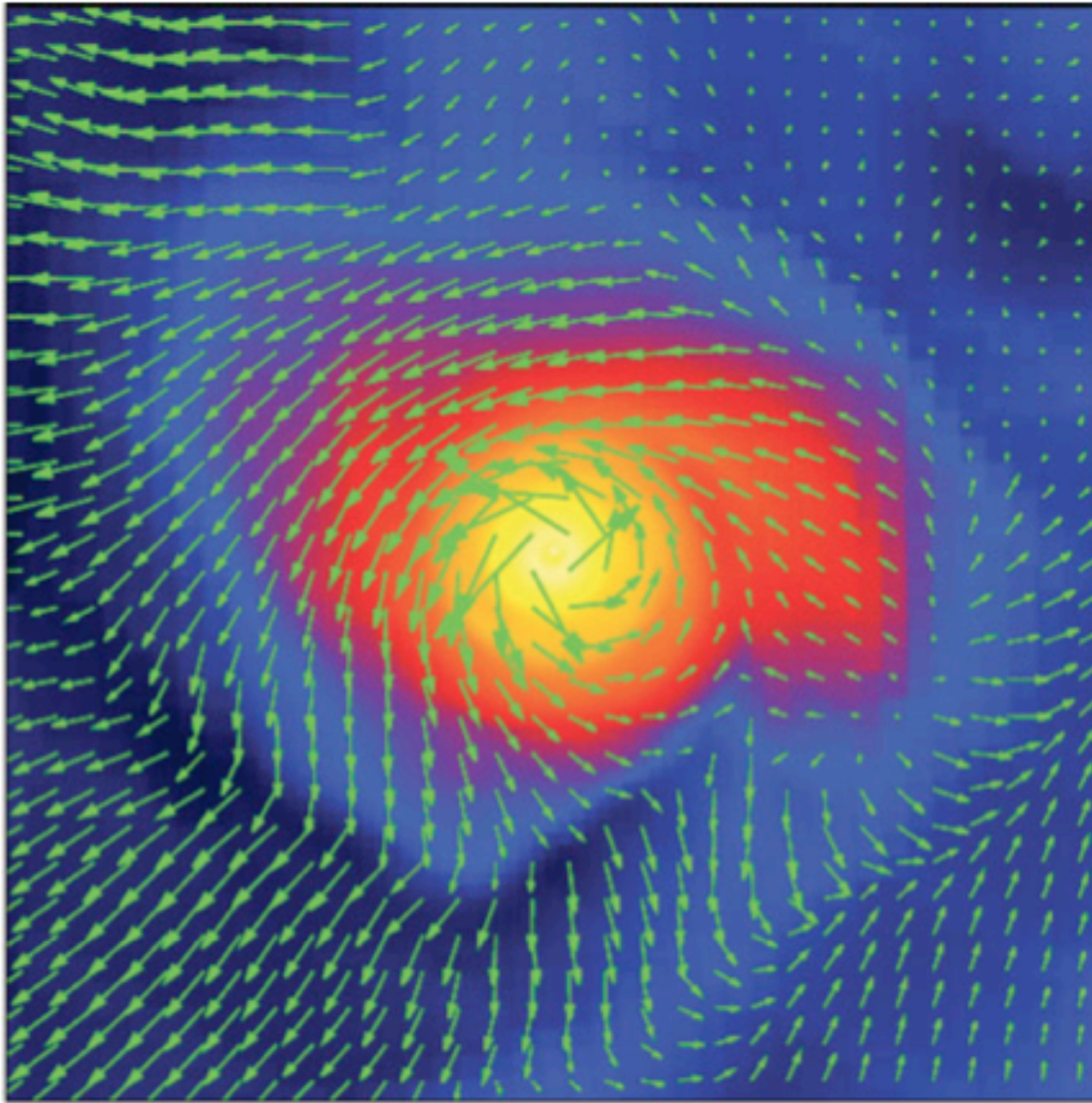
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- low + high mass cores
- strong magnetic field
- with/without global rotation
- sub-/supersonic **turbulence**
- resolution: 1.2 AU

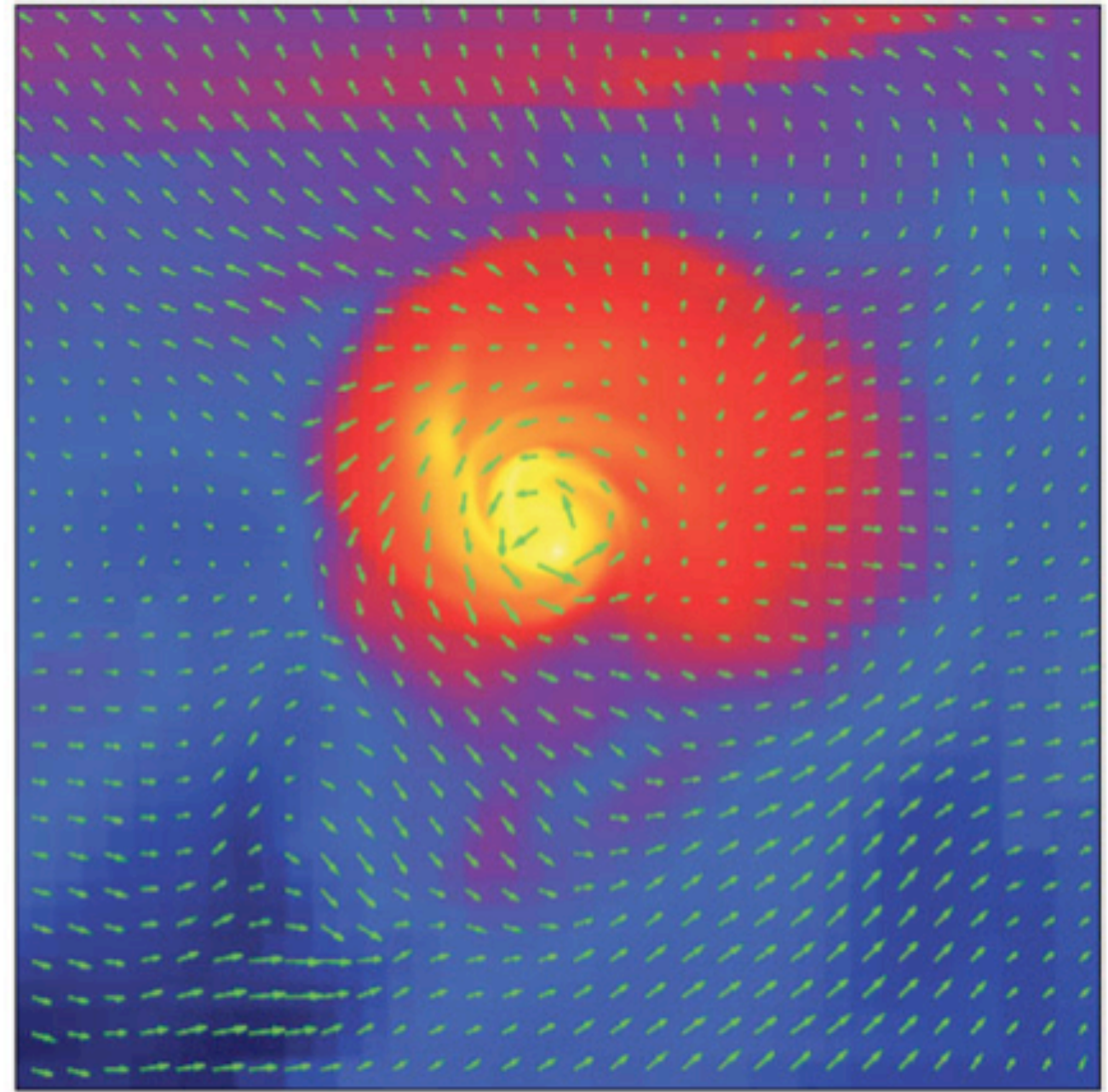
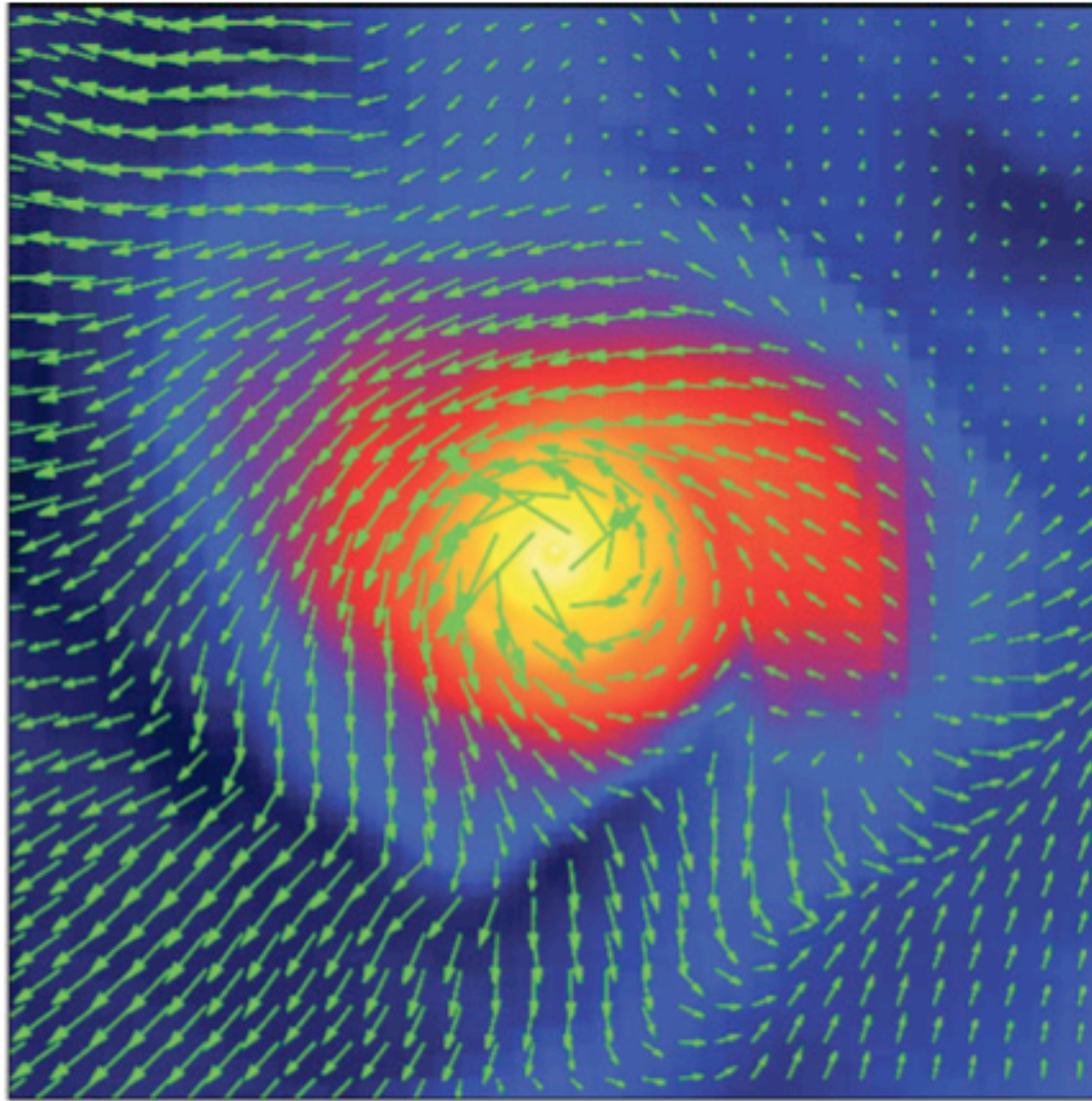


Collapse of Turbulent Cores



Seifried, RB, Pudritz, Klessen 2012

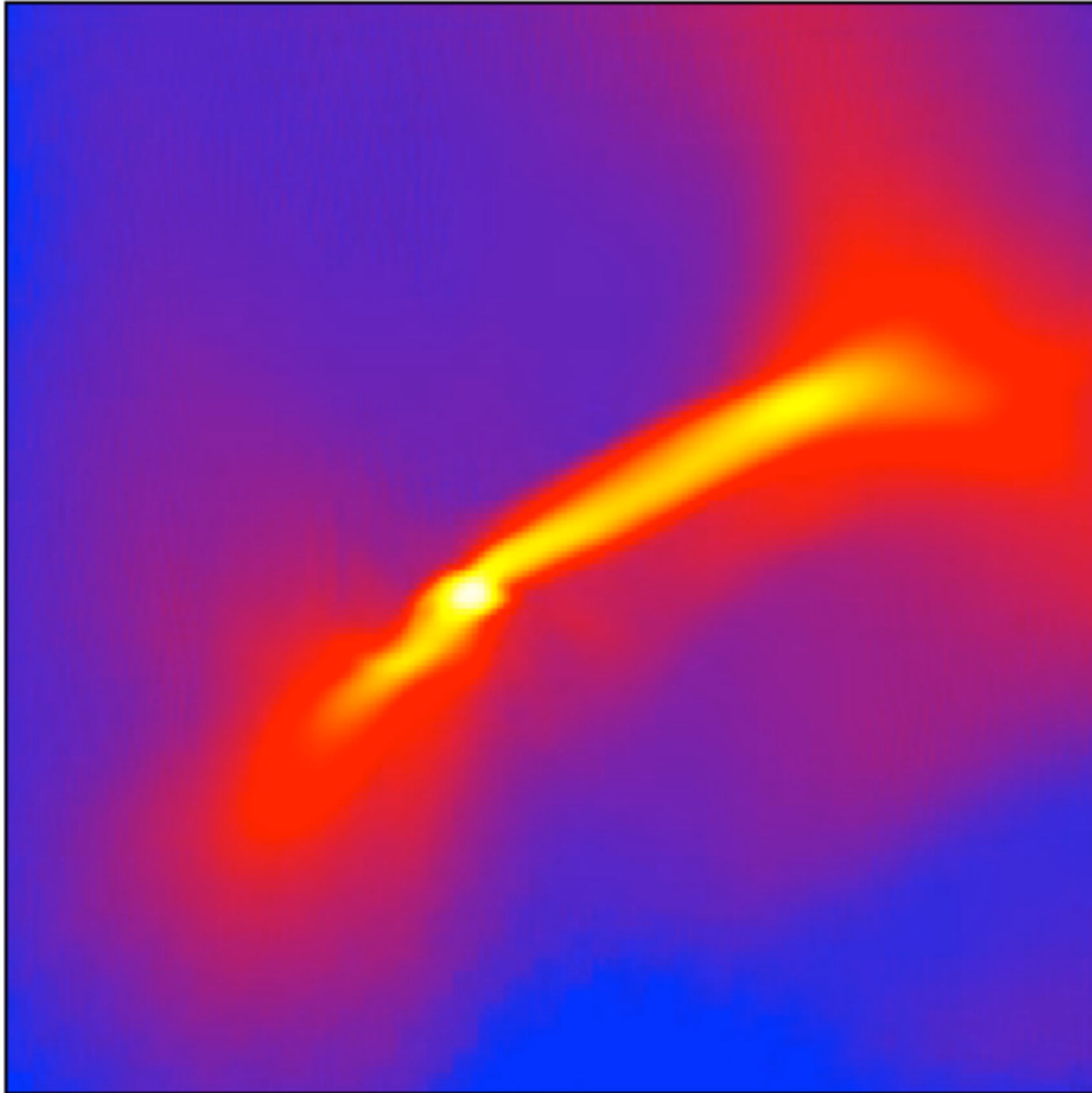
Collapse of Turbulent Cores



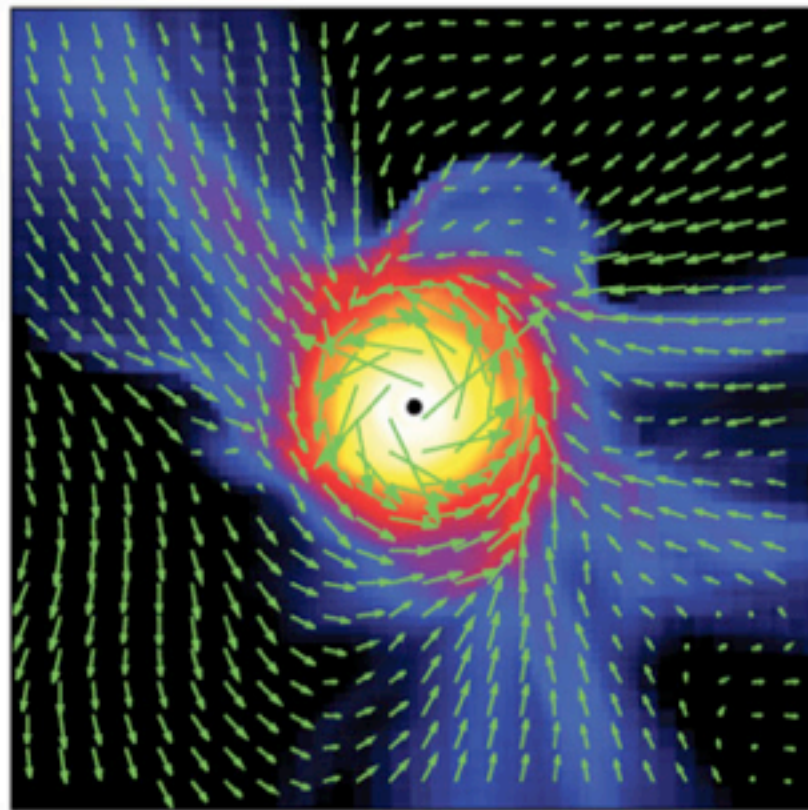
Seifried, RB, Pudritz, Klessen 2012

⇒ discs “reappear”

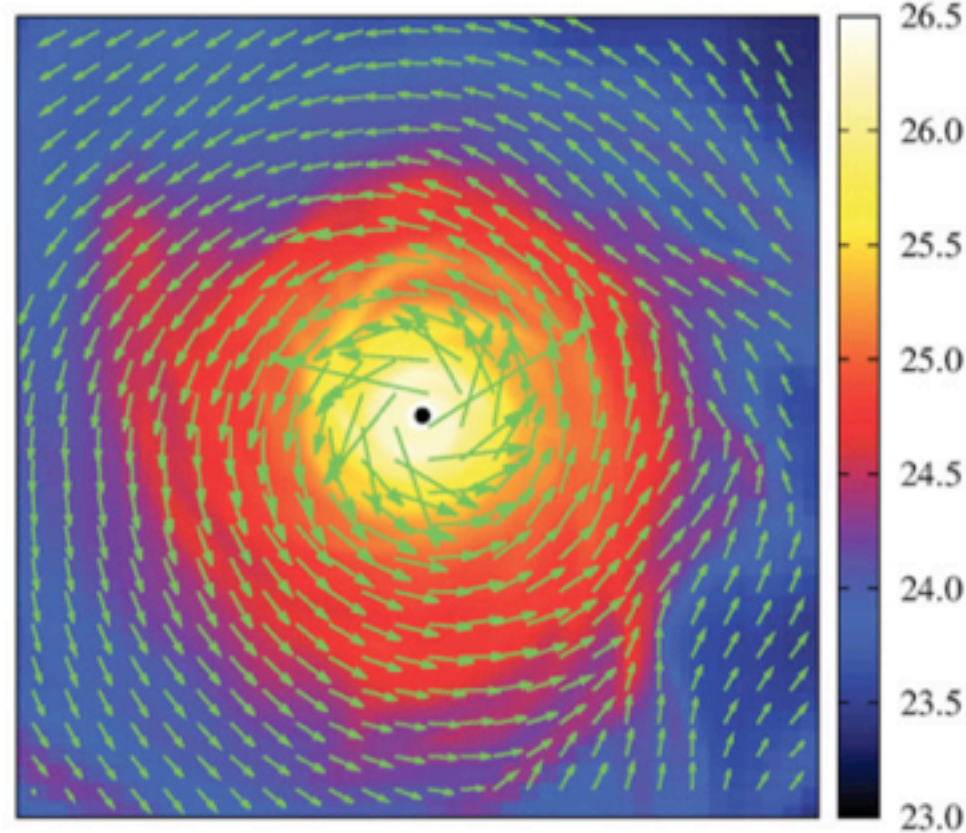
Collapse of Turbulent Cores



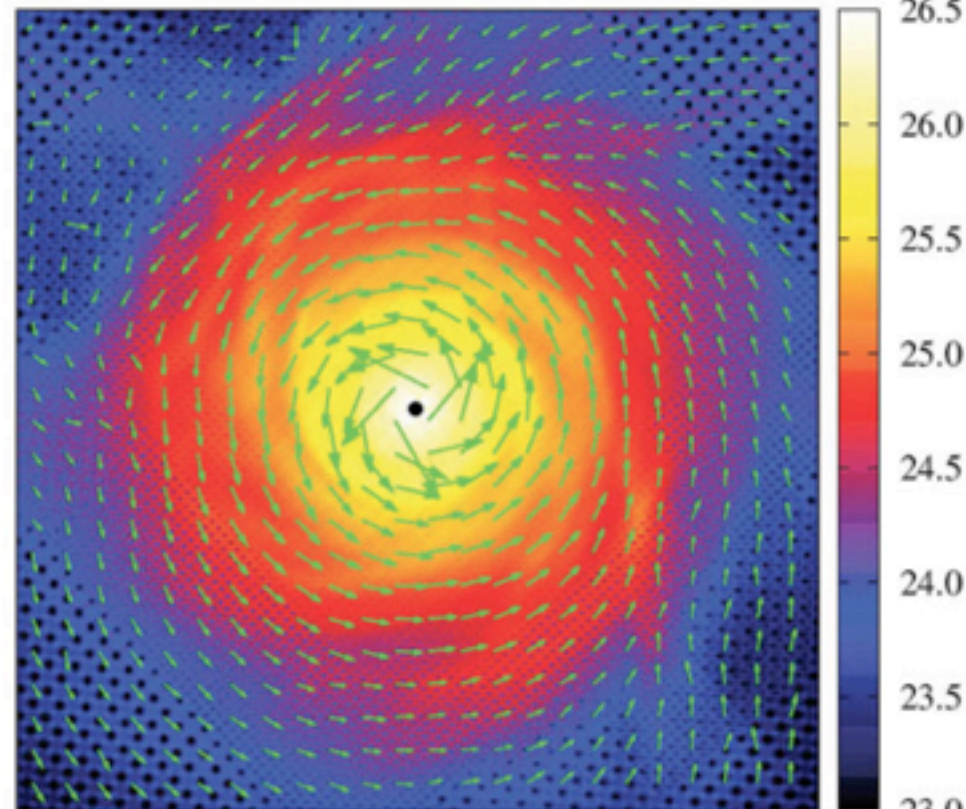
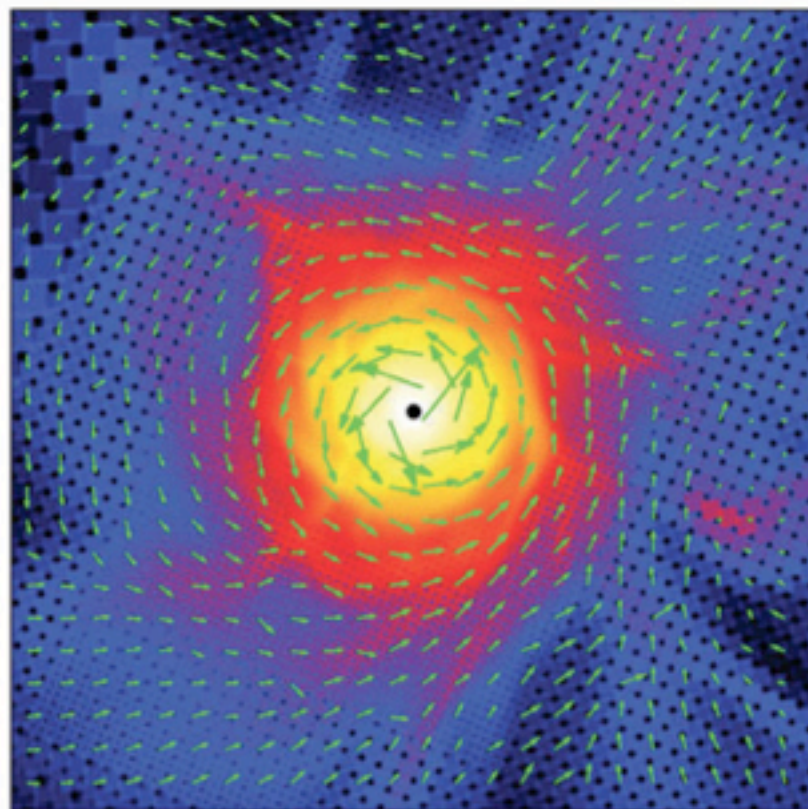
Collapse of Turbulent Cores



200 AU



- low mass cores
- strong magnetic field: $\mu = 2.6 \mu_{\text{crit}}$
- transonic turbulence $Ma = 0.74$
- **no** global rotation

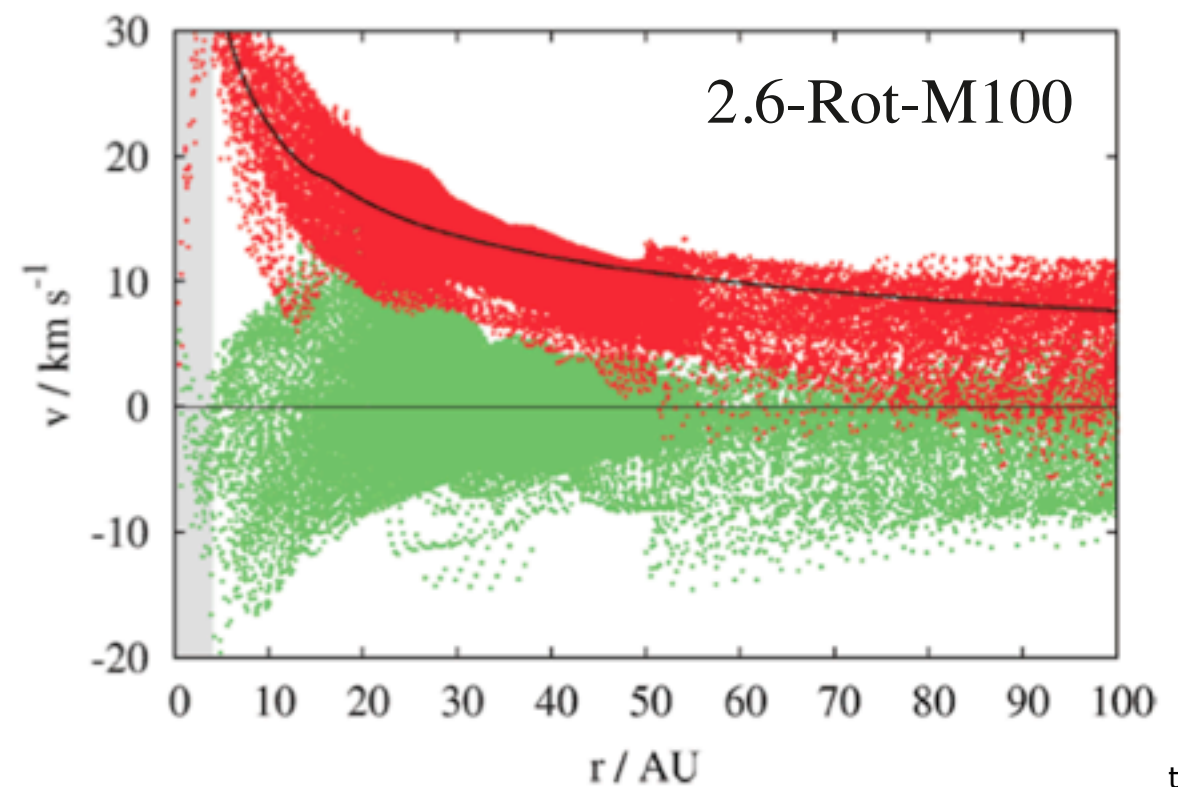
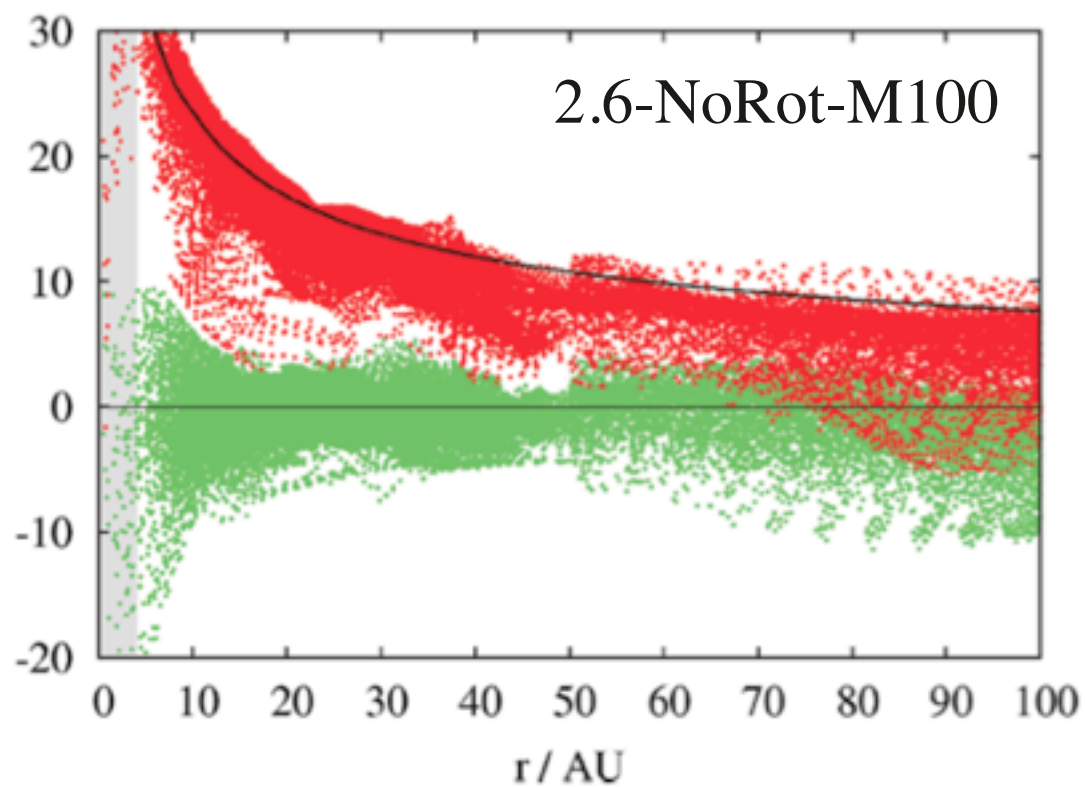
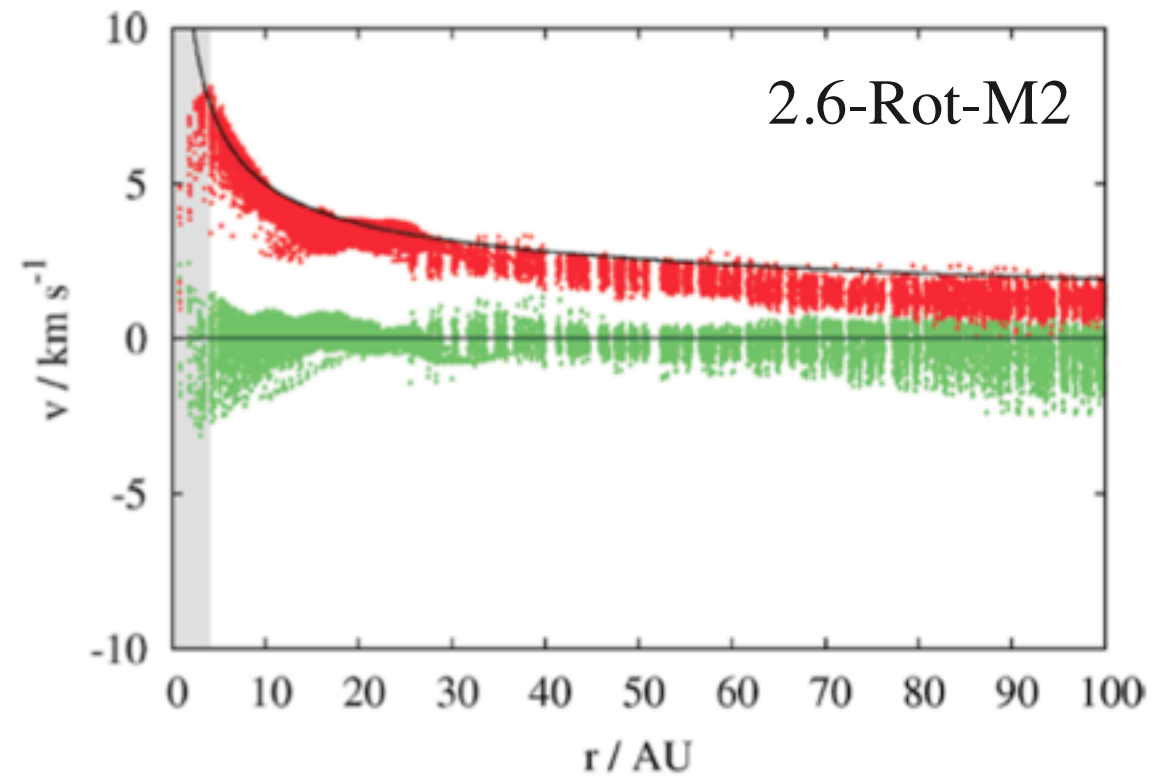
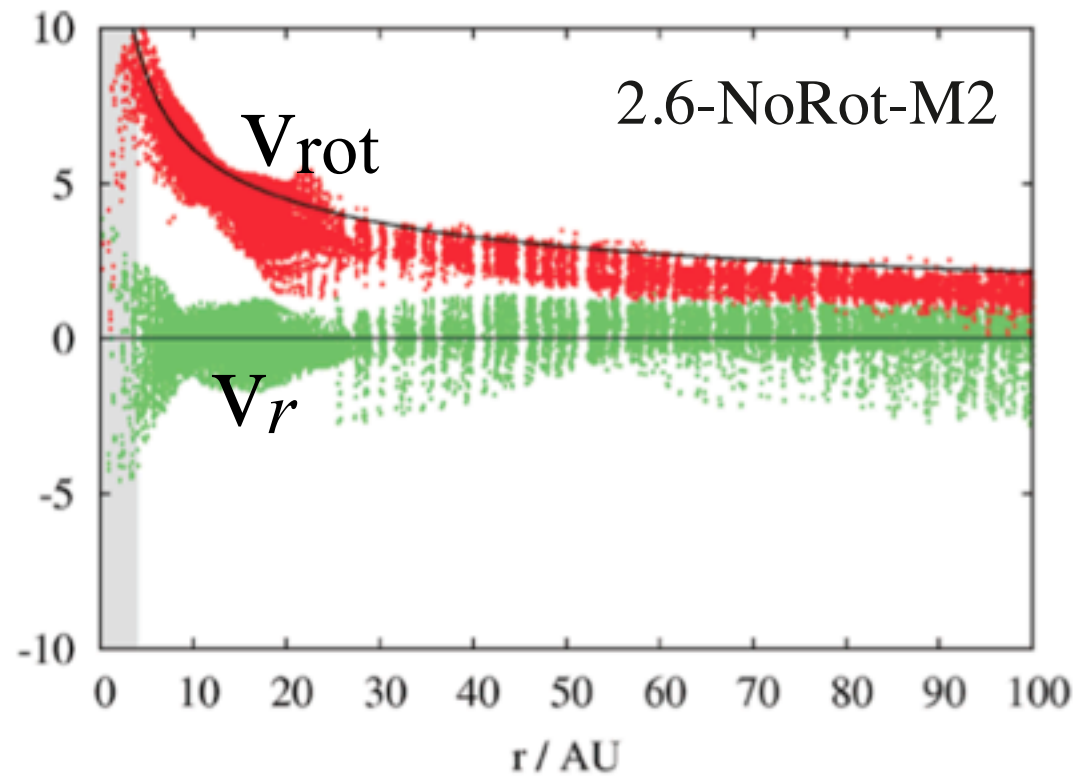


- with global rotation

Seifried, et al. 2013

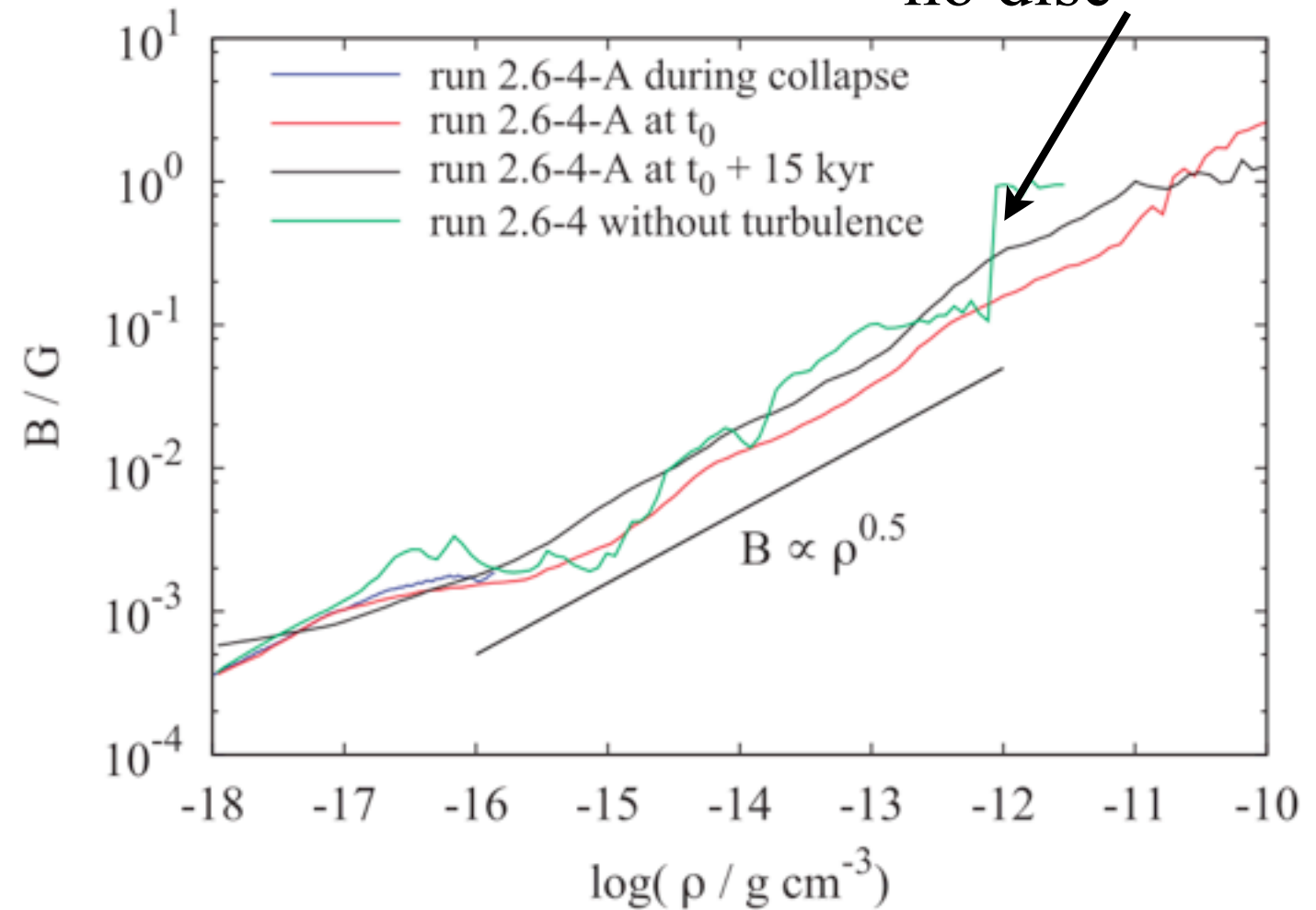
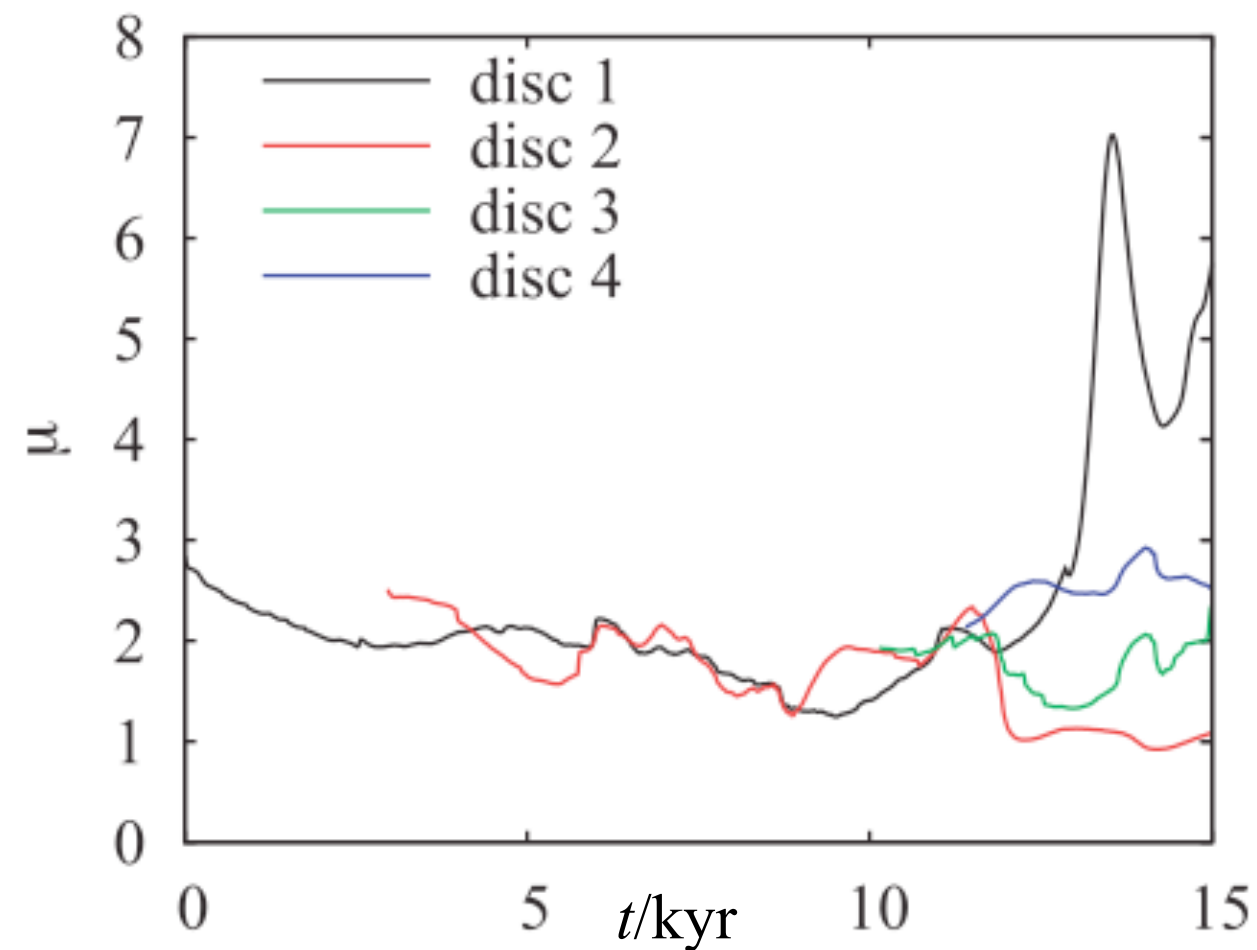
Collapse of Turbulent Cores

velocity structure



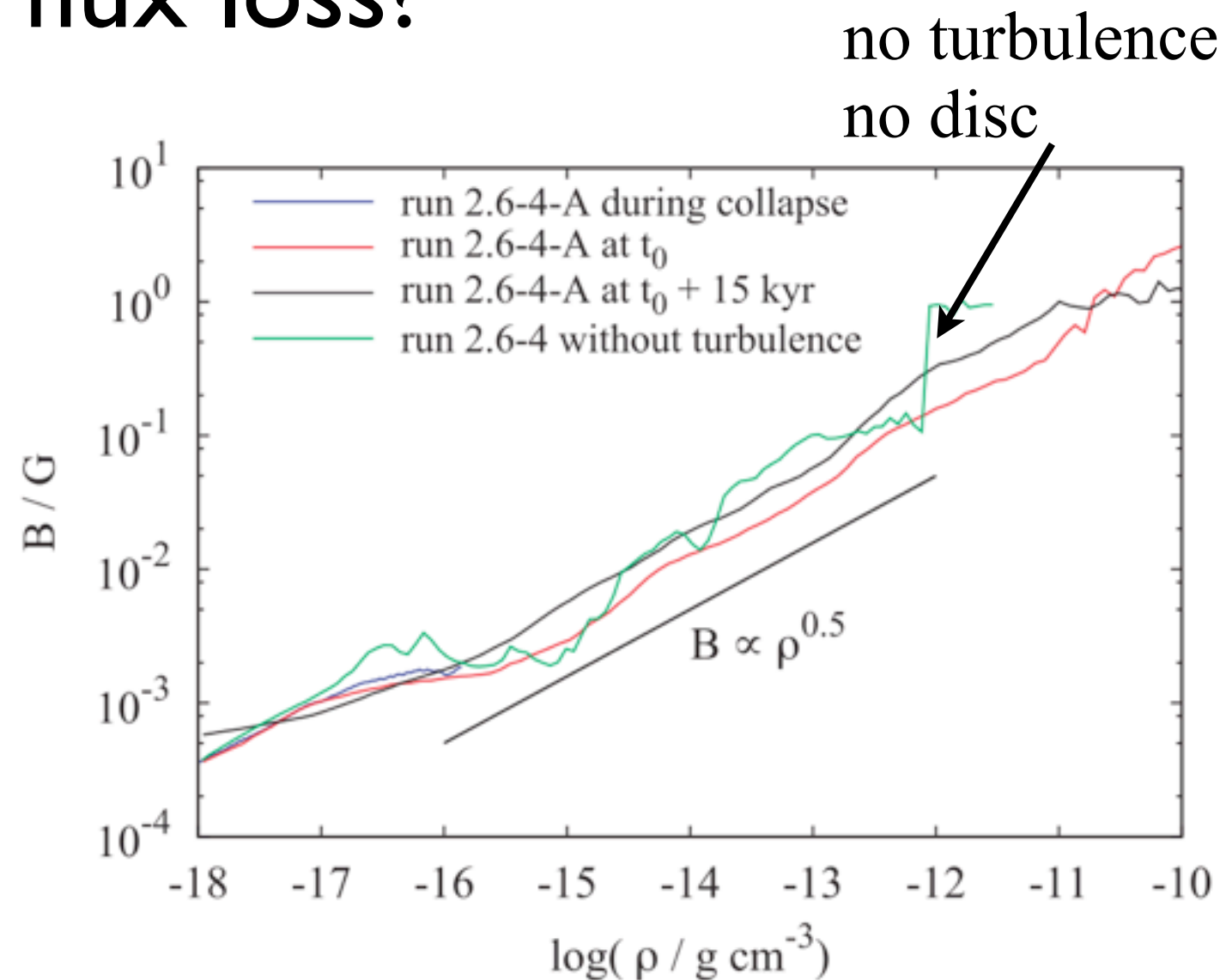
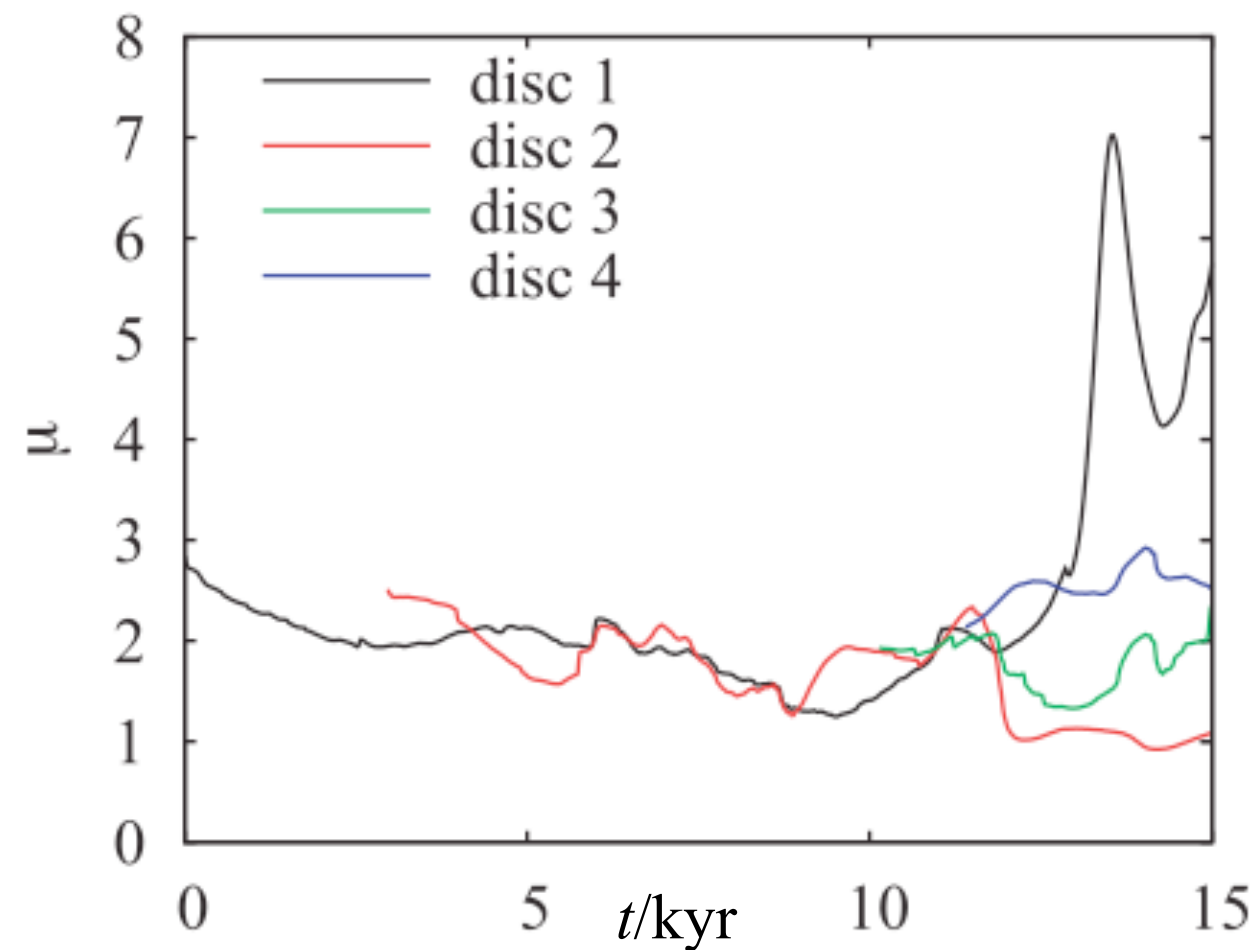
Collapse of Turbulent Cores

due to flux loss?



Collapse of Turbulent Cores

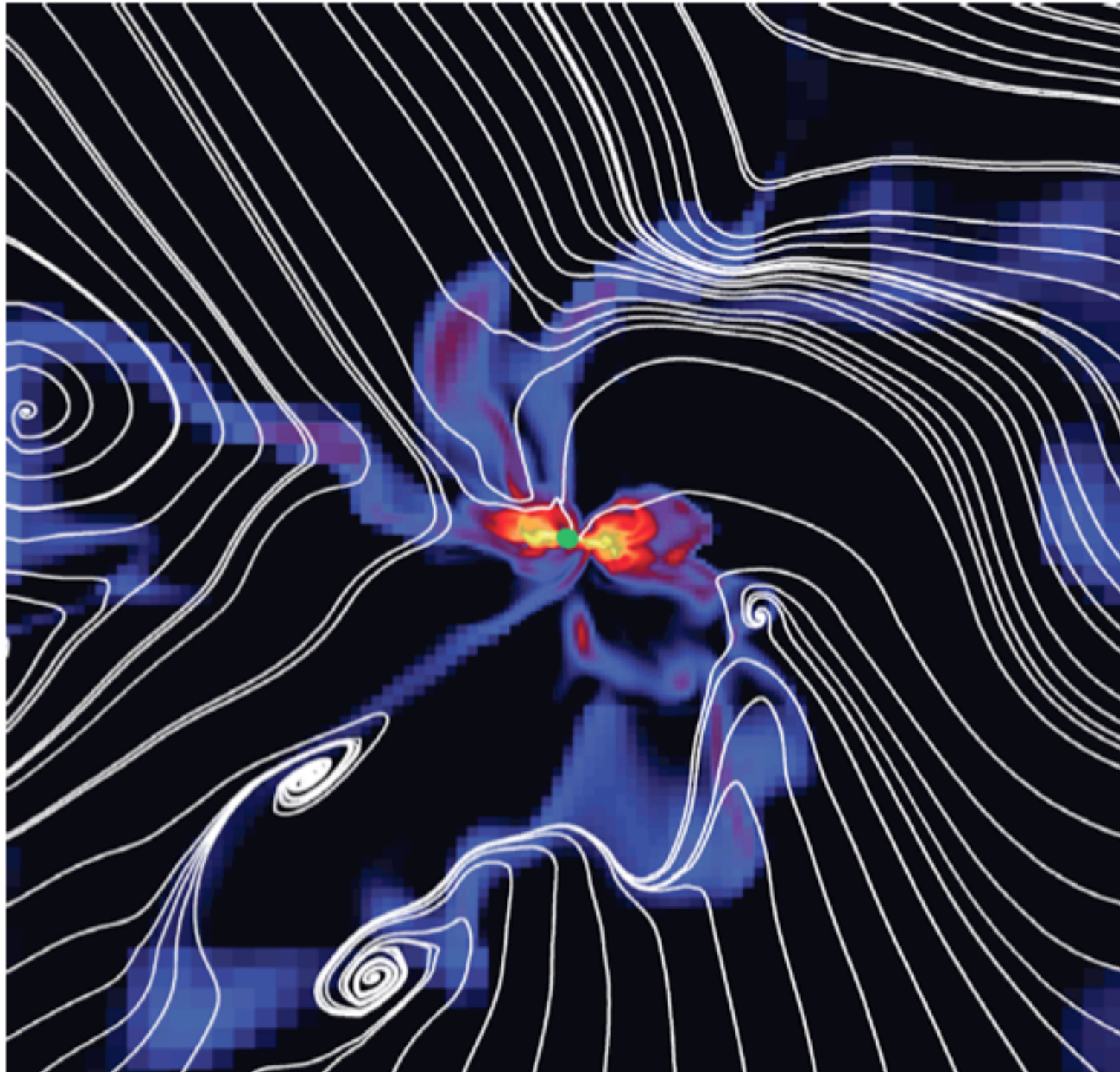
due to flux loss?



$\Rightarrow$ only little flux loss

Collapse of Turbulent Cores

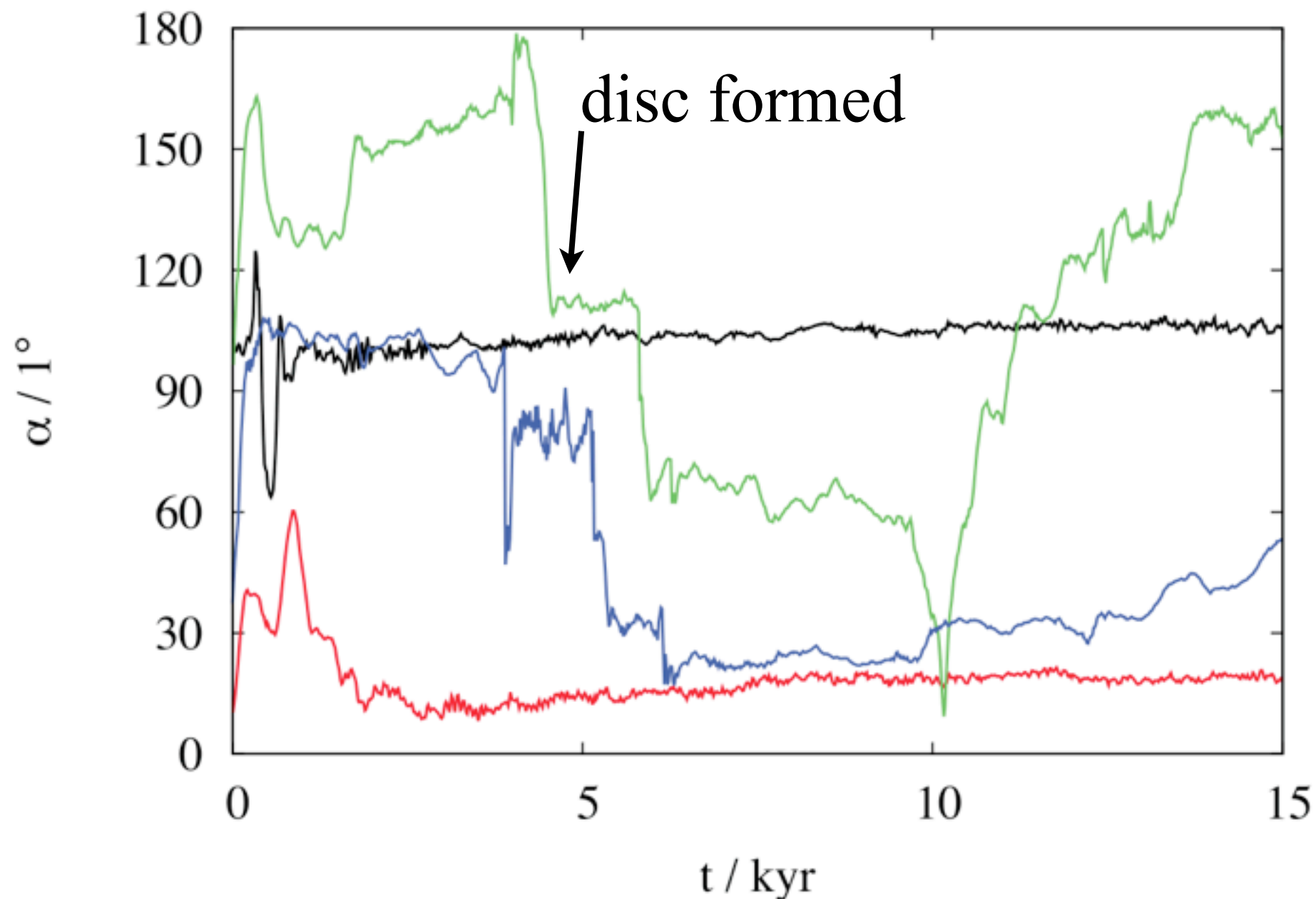
Magnetic field structure



Collapse of Turbulent Cores

rotation vs. magnetic field orientation
 $\Rightarrow$ inclined rotation helps to form discs?

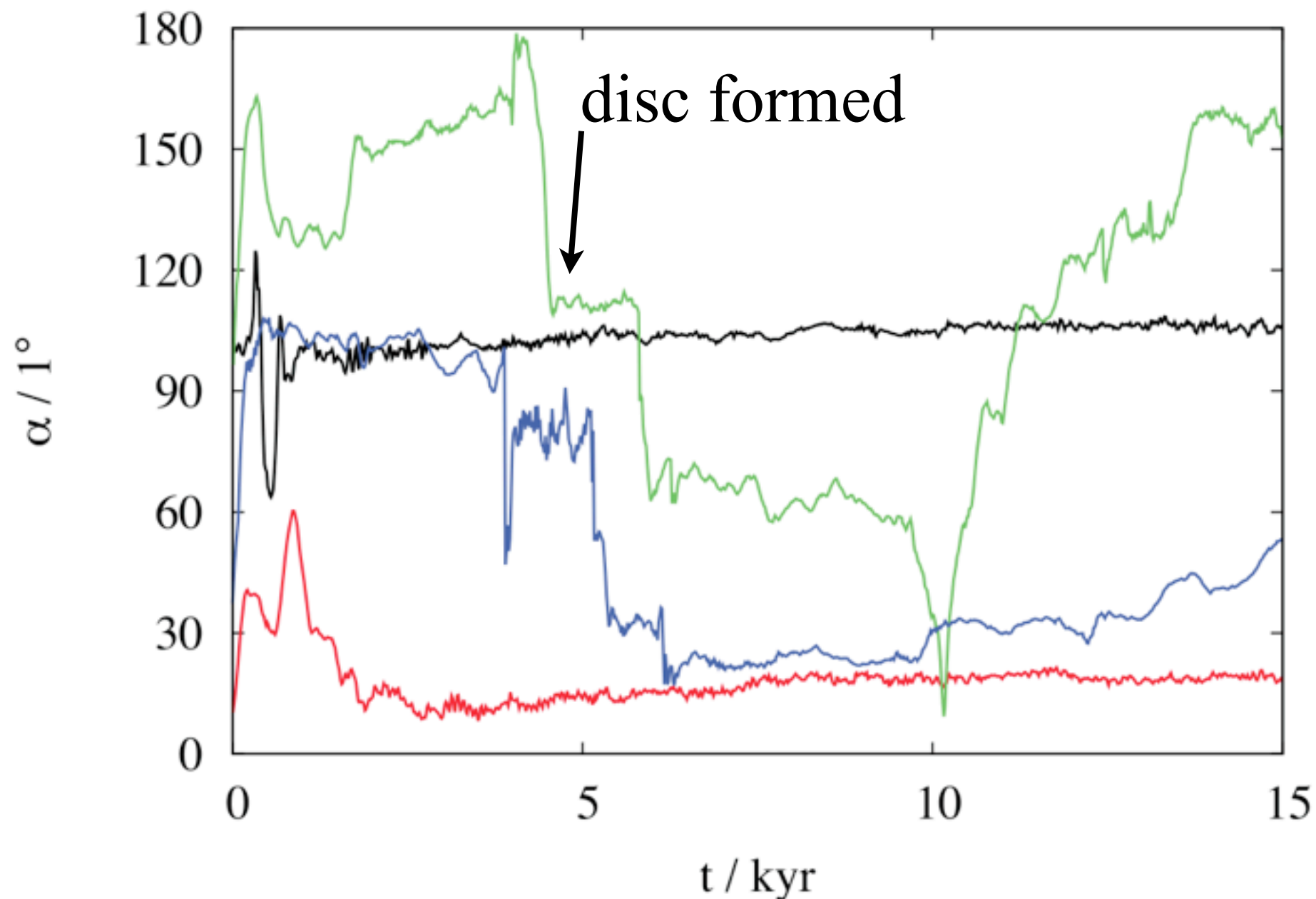
(Hennbelle & Ciardi 2009, Joos et al. 2012)



Collapse of Turbulent Cores

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 $\Rightarrow$ inclined rotation helps to form discs?

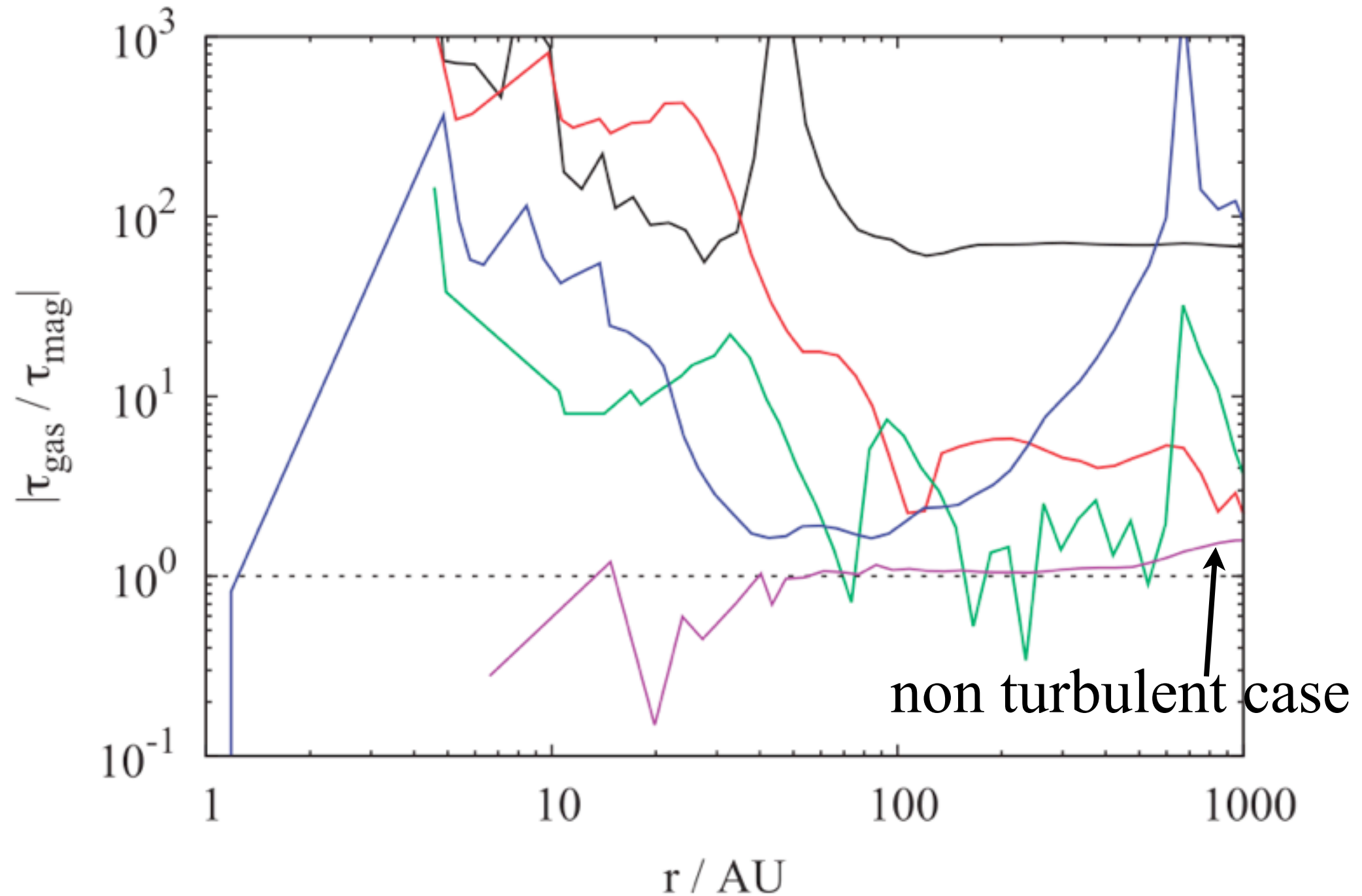
(Hennbelle & Ciardi 2009, Joos et al. 2012)



$\Rightarrow$ but no large
scale magnetic
field component

Collapse of Turbulent Cores

Torques



Summary

- It is easy to form discs
- Angular momentum is efficiently transported during disc formation by gravitational torques
- Magnetic braking catastrophe only for **unrealistic** ICs